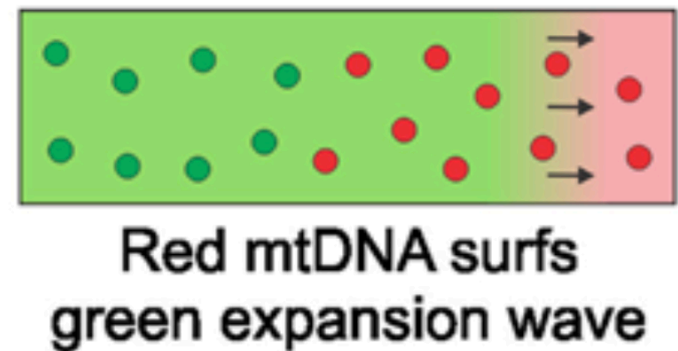
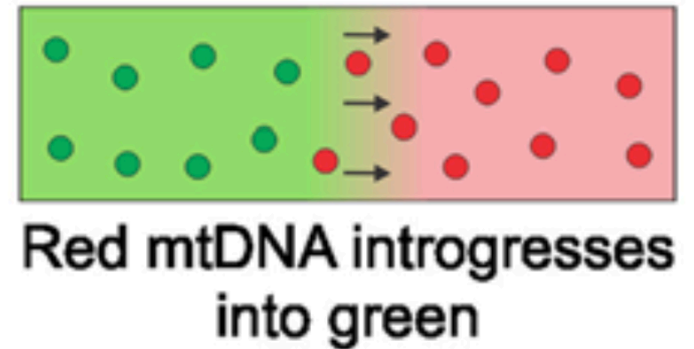
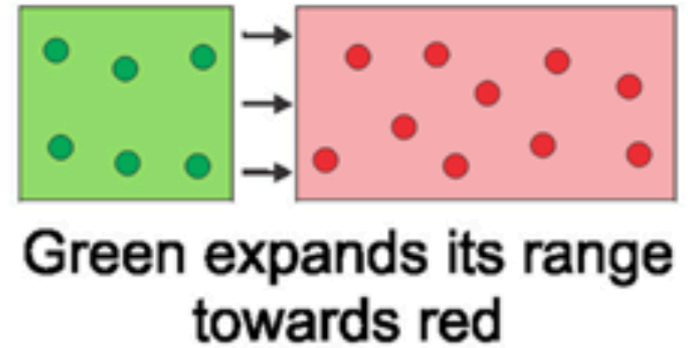
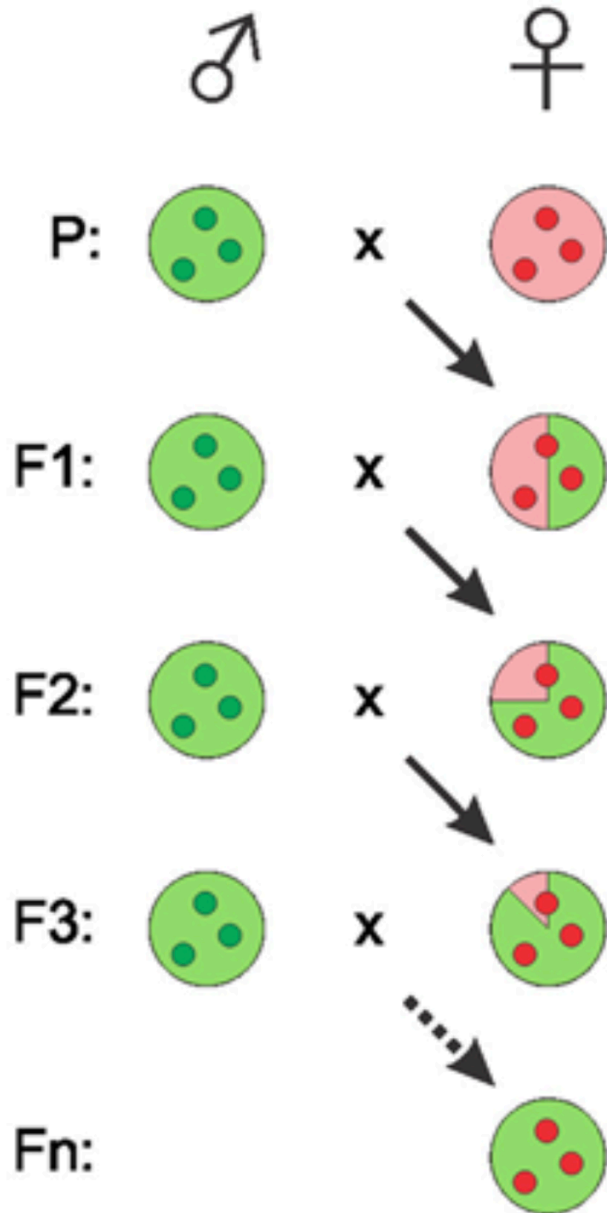
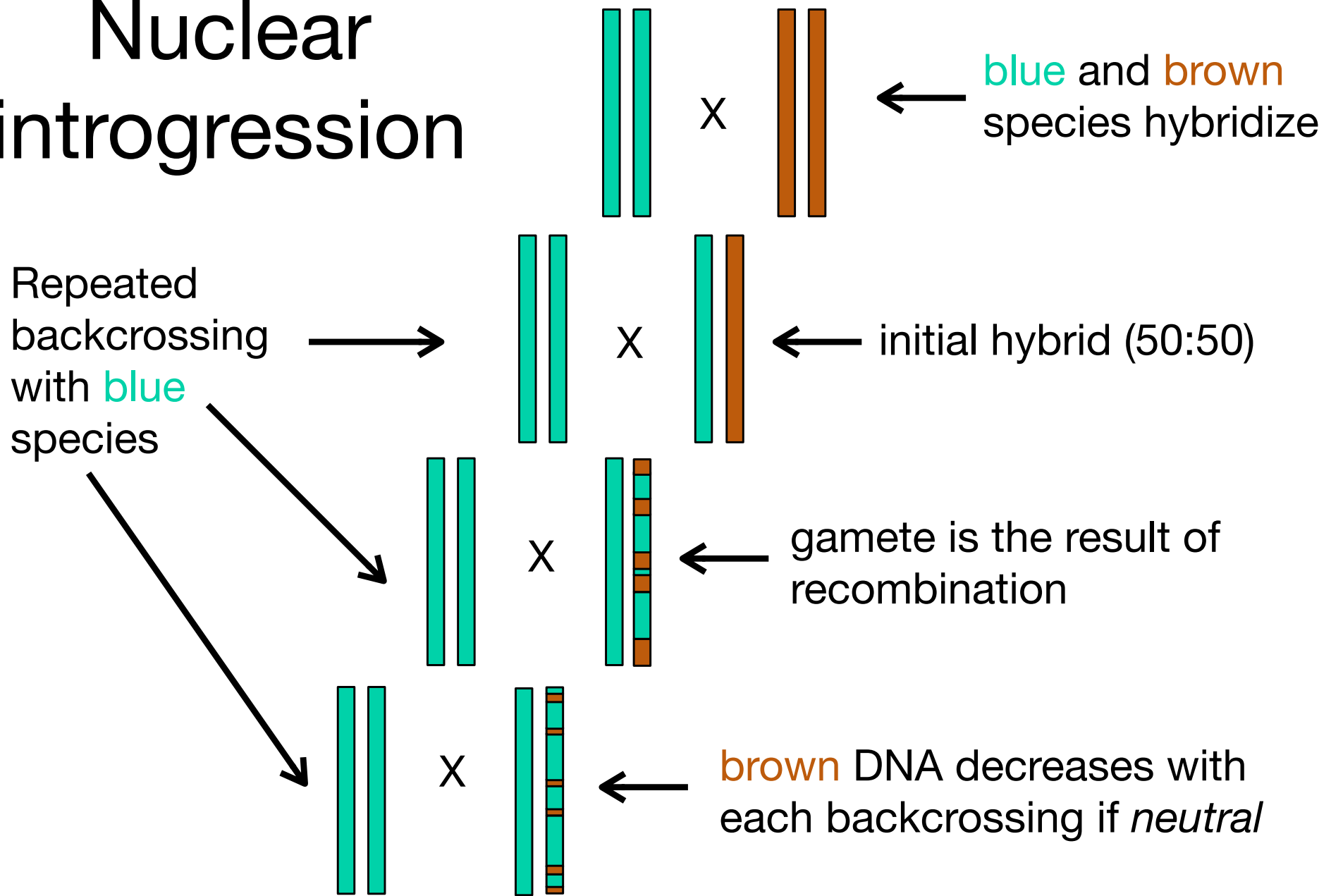


# Introgression, hybridization, and phylogenetic networks

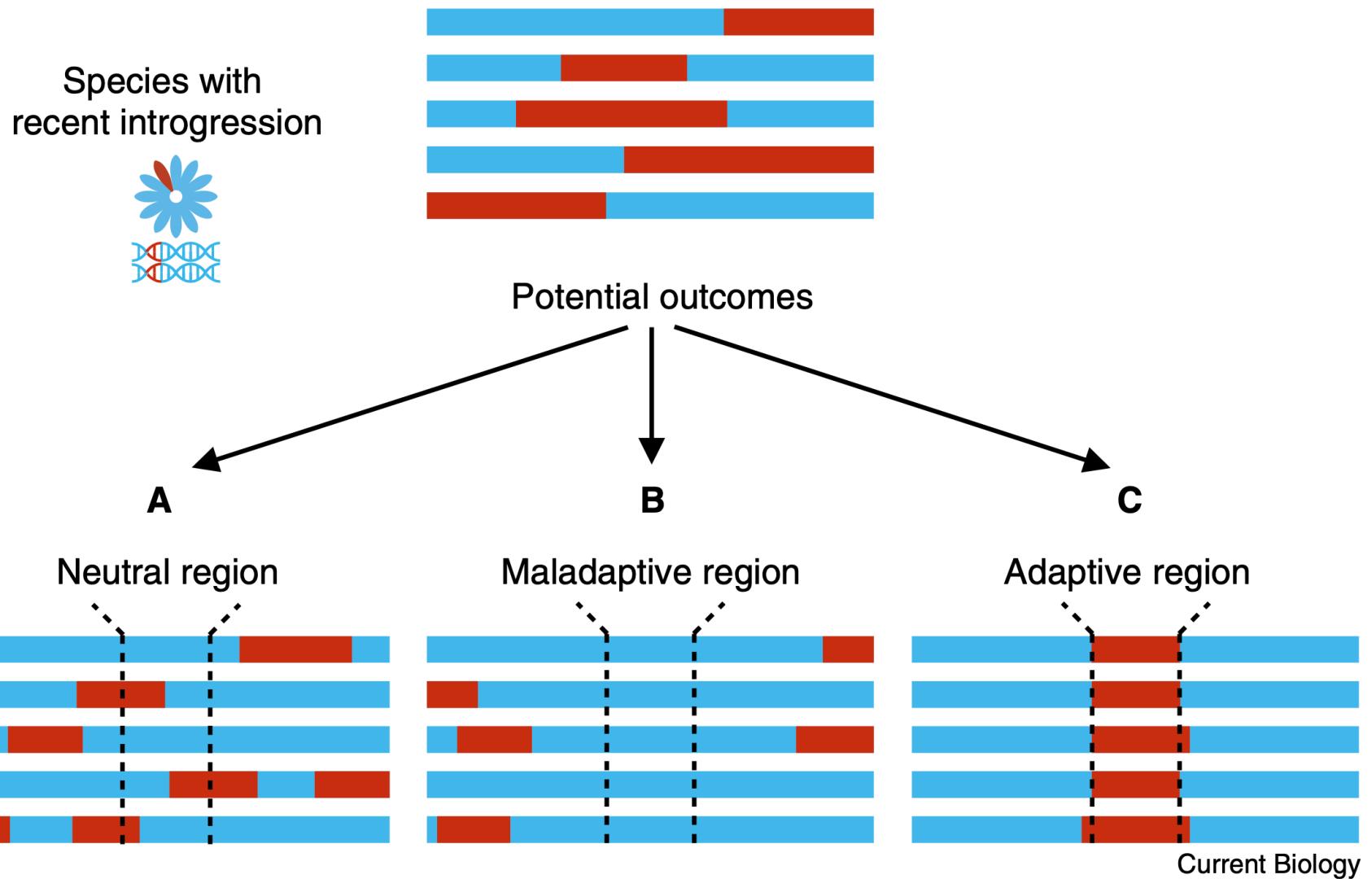
# Mitochondrial introgression

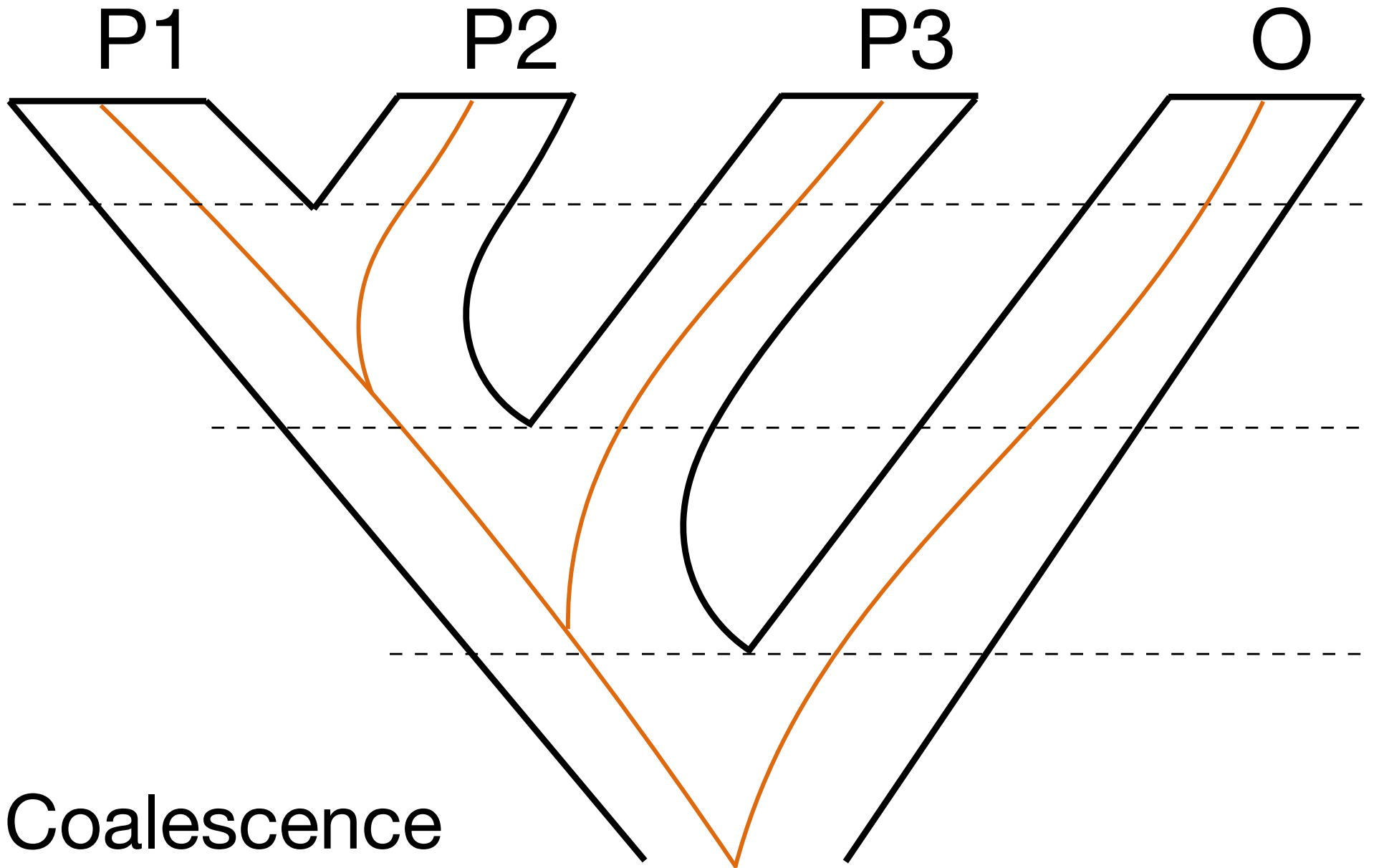


# Nuclear introgression

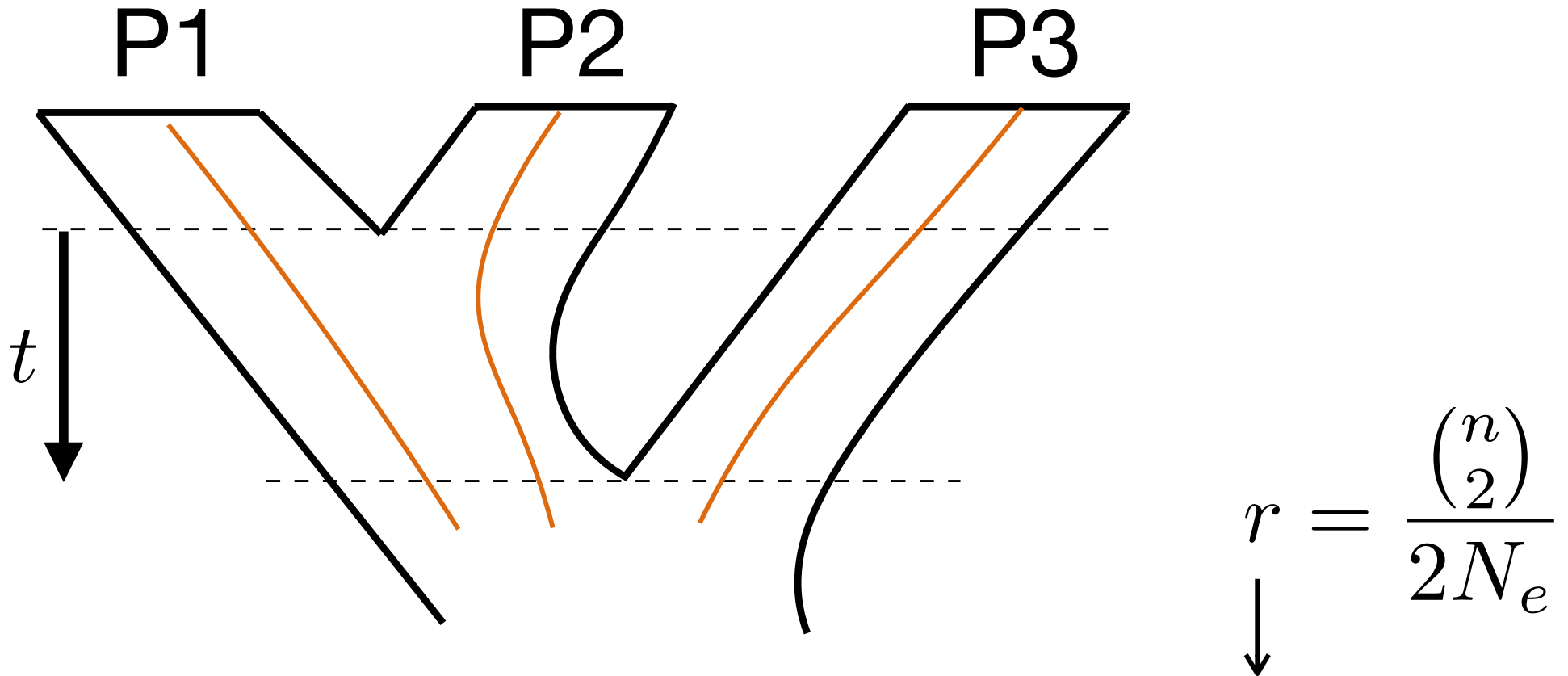


# Nuclear introgression





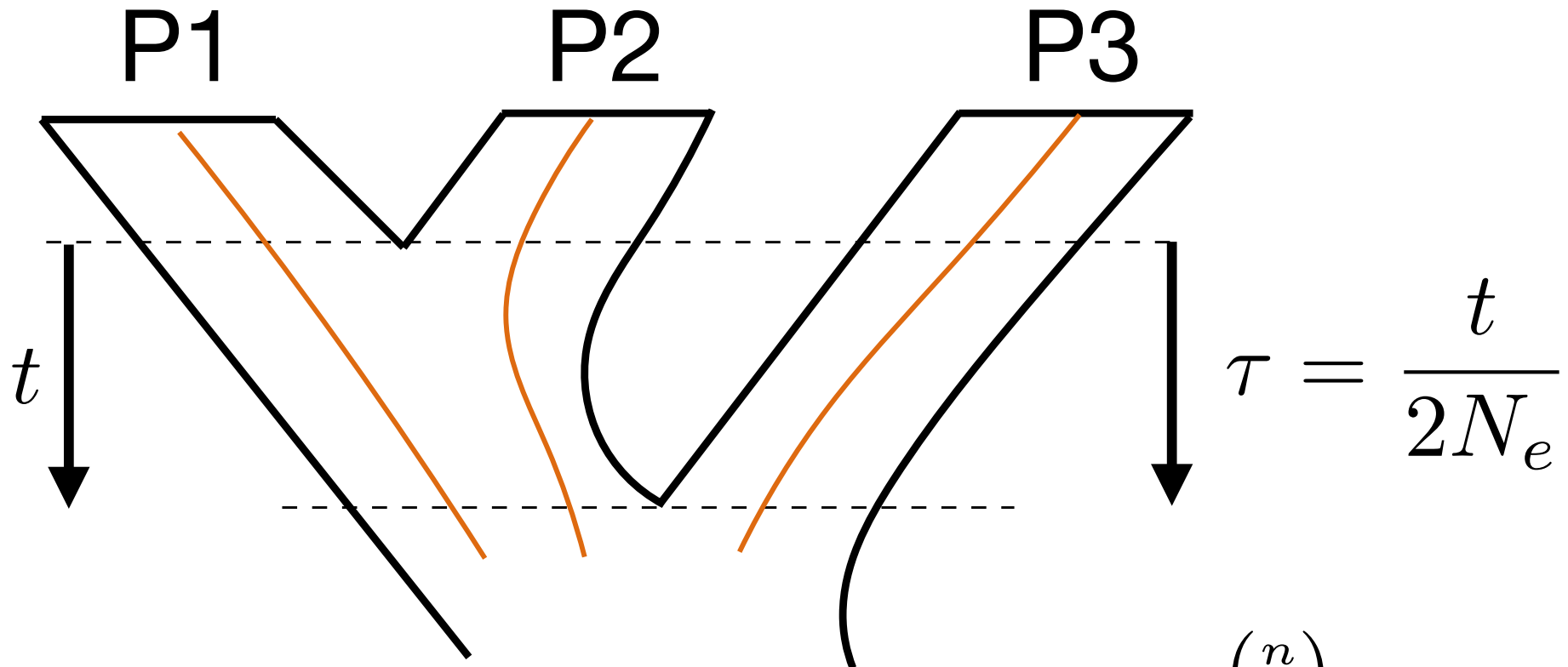
# Probability of coalescence



$$p(\text{coal. by time } t) = 1 - e^{-rt}$$
$$p(\text{no coal. by time } t) = e^{-rt}$$

$$r = \frac{\binom{n}{2}}{2N_e}$$

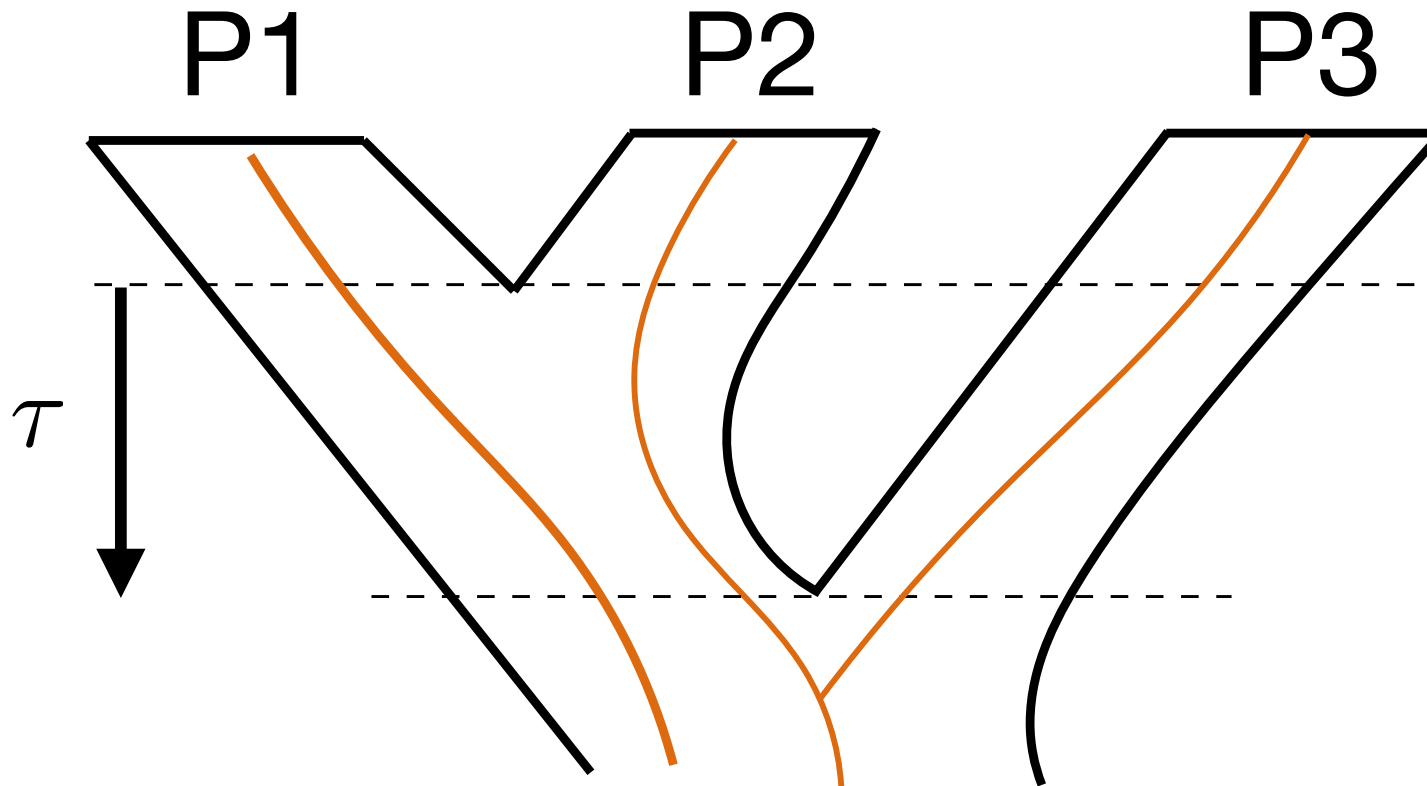
# Probability of coalescence



$$p(\text{no coal. by time } t) = e^{-\frac{\binom{n}{2}}{2N_e} t}$$

$$p(\text{no coal. by time } \tau) = e^{-\tau}$$

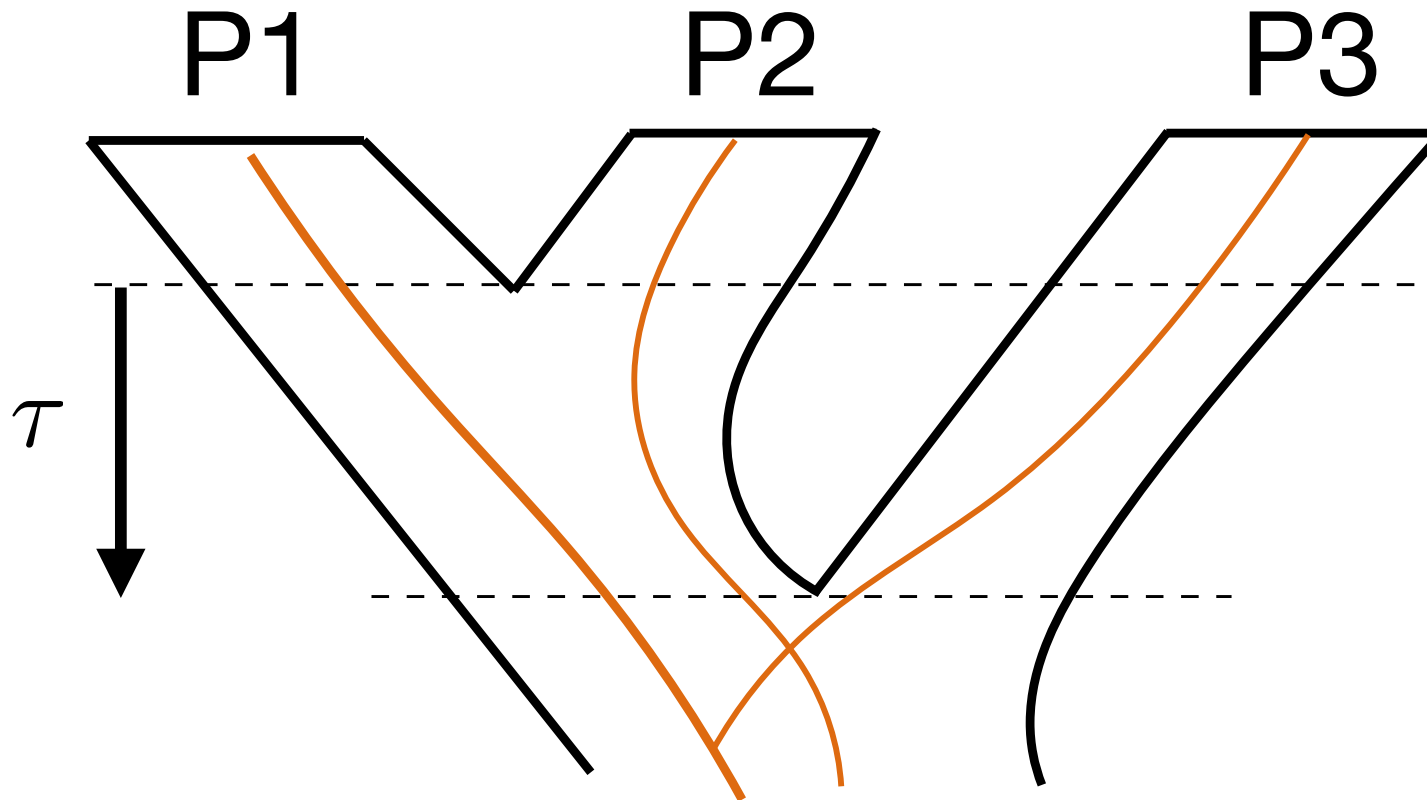
# Probability of **conflicting** topology



Prob(no coalescence AND P2 joins with P3)

$$= \frac{1}{3} e^{-\tau}$$

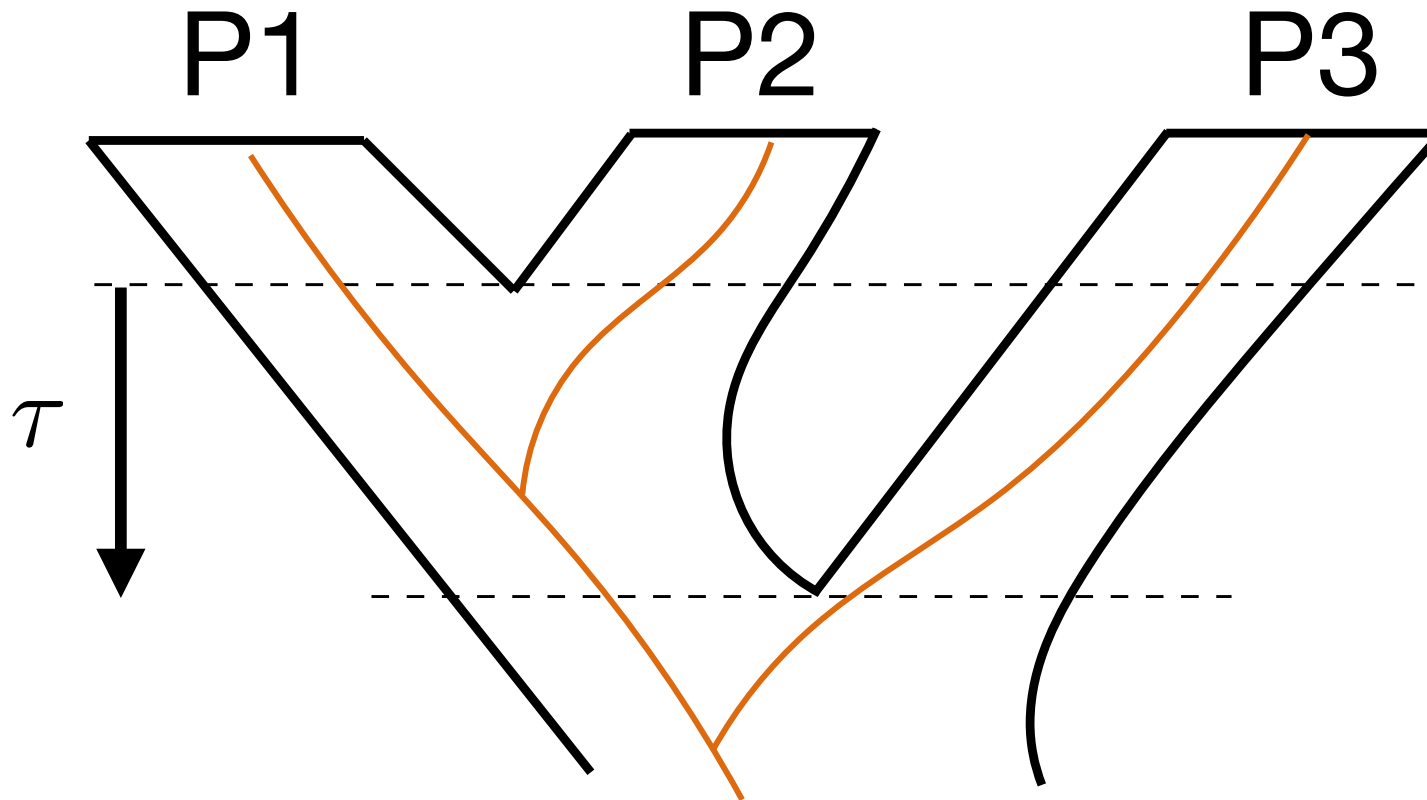
# Probability of **conflicting** topology



Prob(no coalescence AND P1 joins with P3)

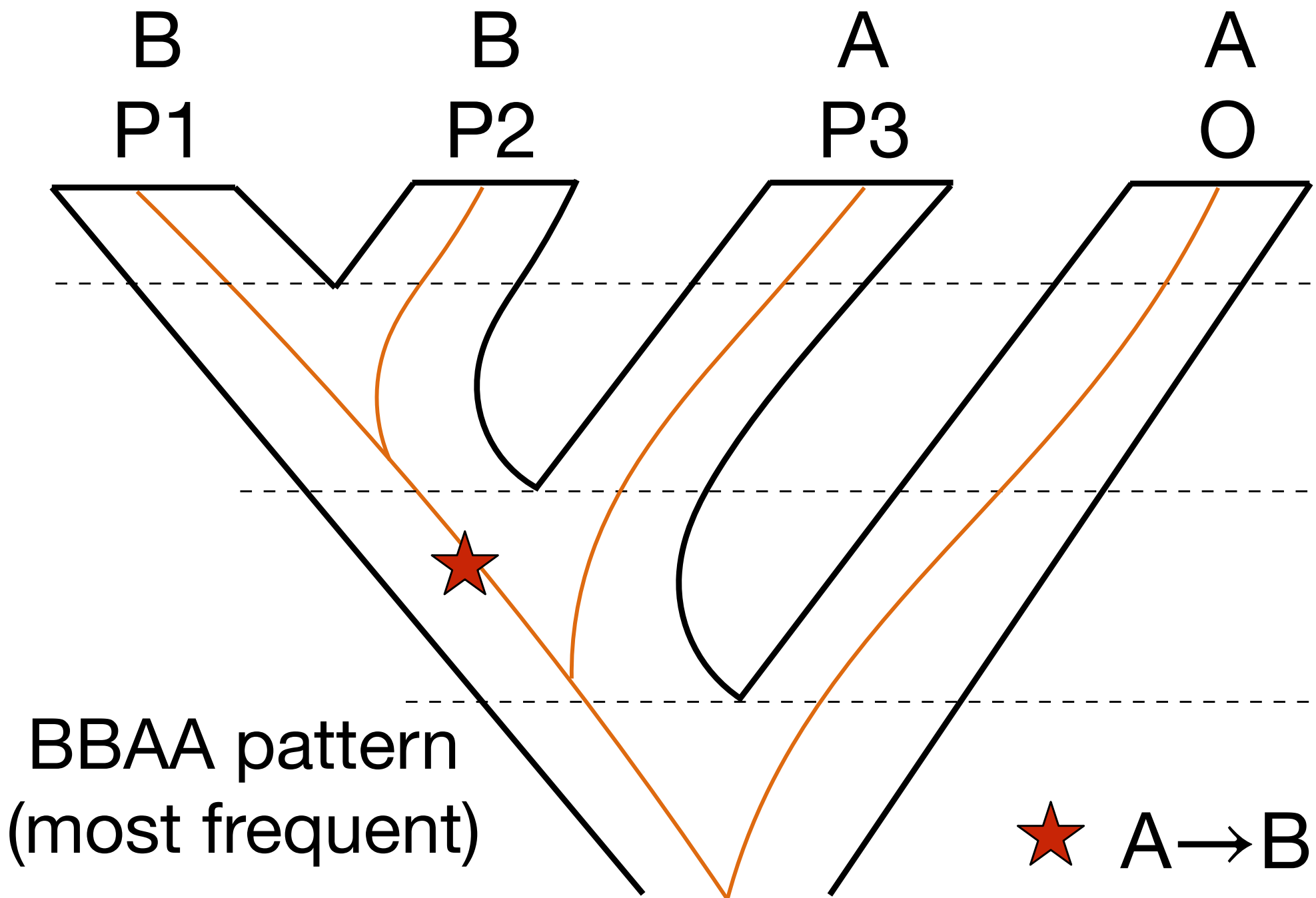
$$= \frac{1}{3} e^{-\tau}$$

# Probability of **compatible** topology



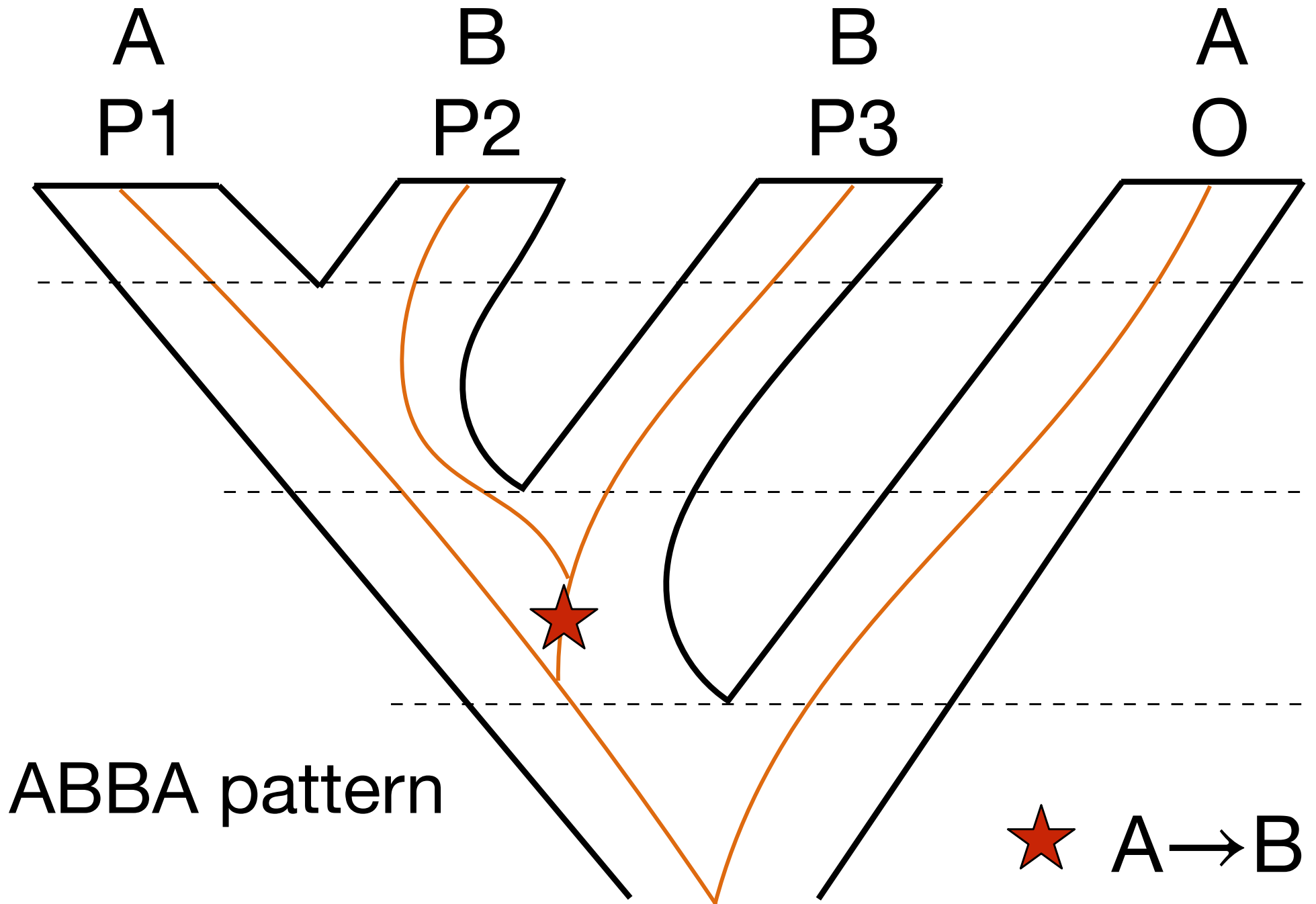
Prob(coalescence OR P1 joins with P2 anyway)

$$= (1 - e^{-\tau}) + \frac{1}{3}e^{-\tau} = 1 - \frac{2}{3}e^{-\tau}$$



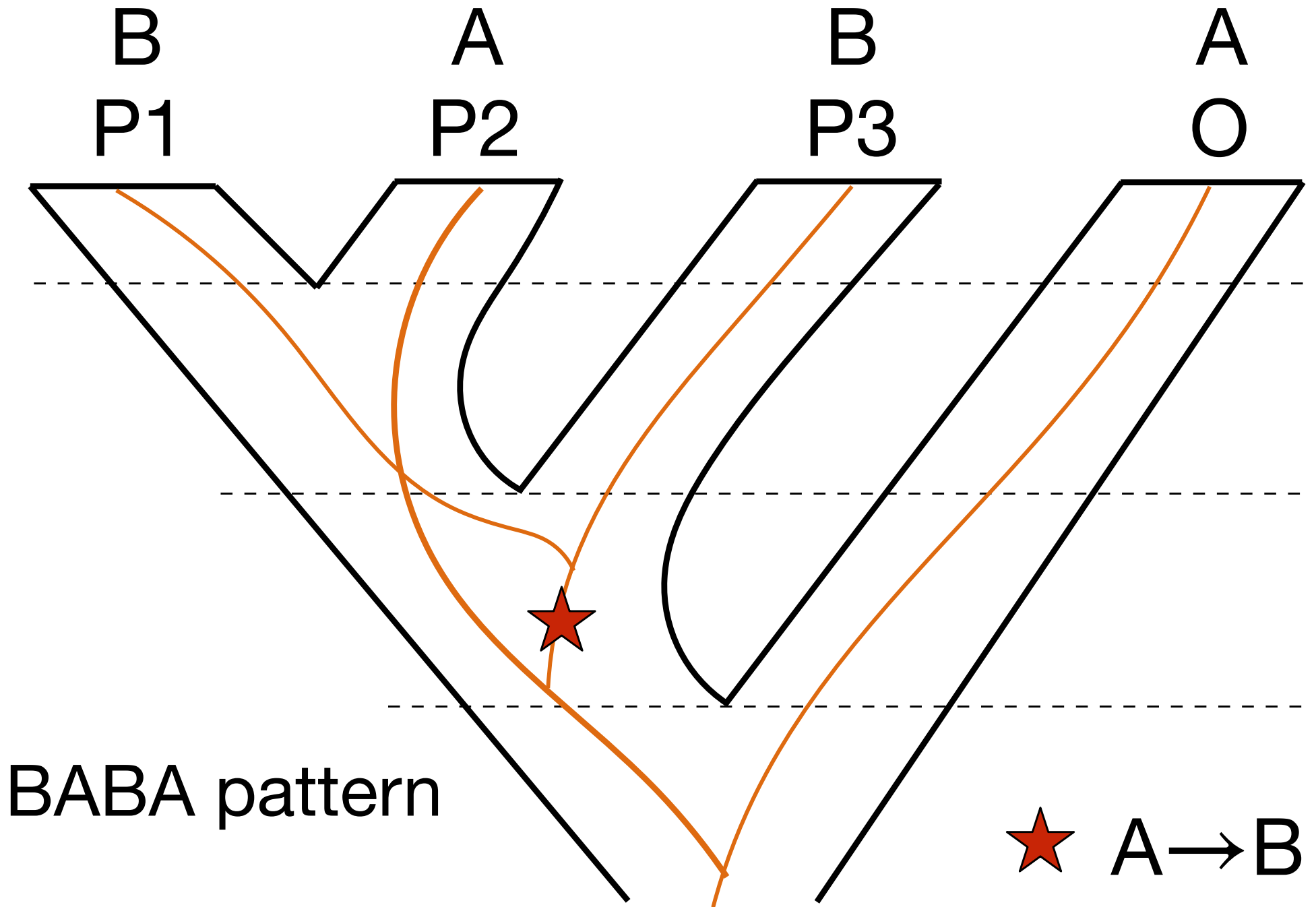
**BBAA pattern  
(most frequent)**

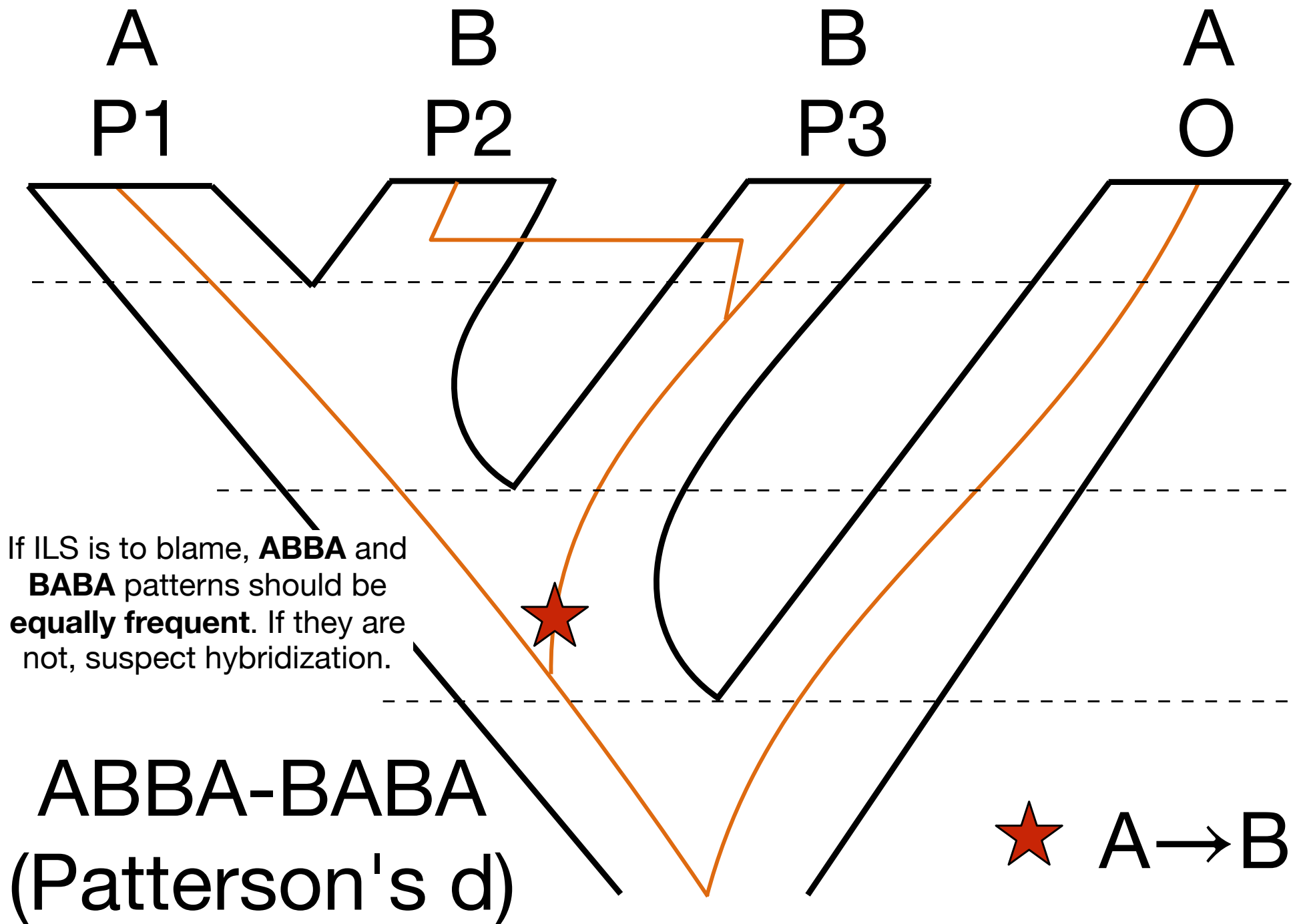
**★ A → B**

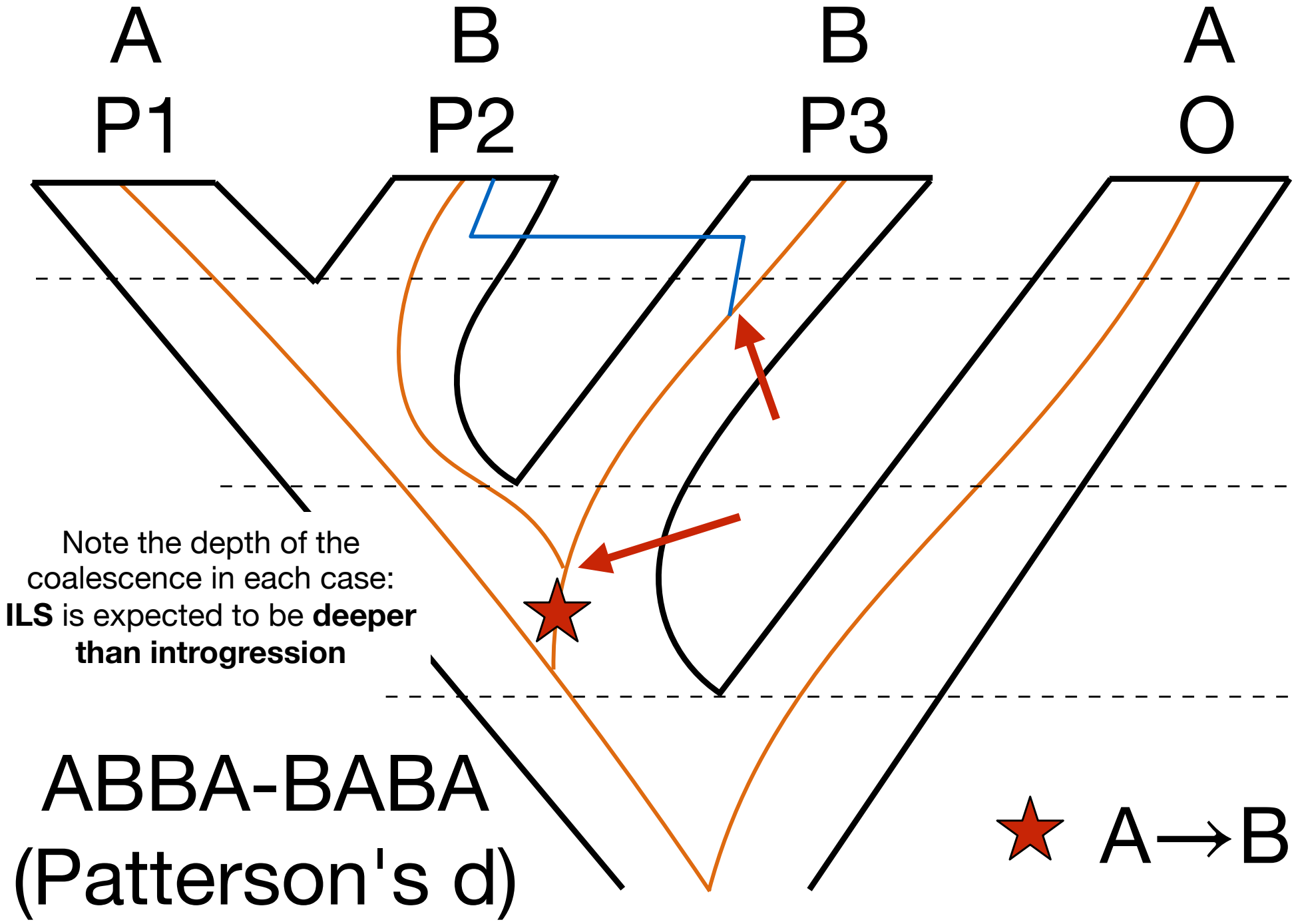


ABBA pattern

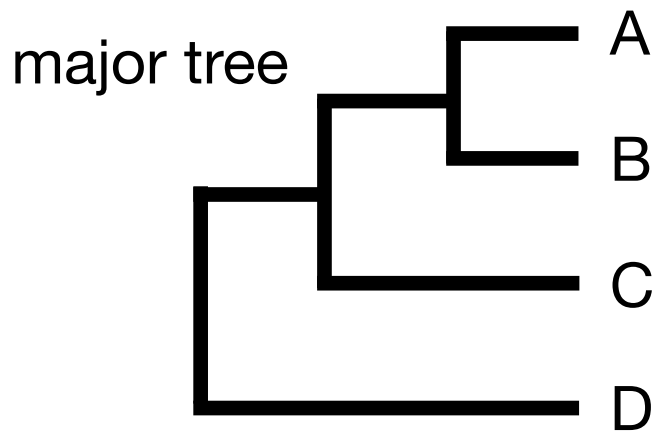
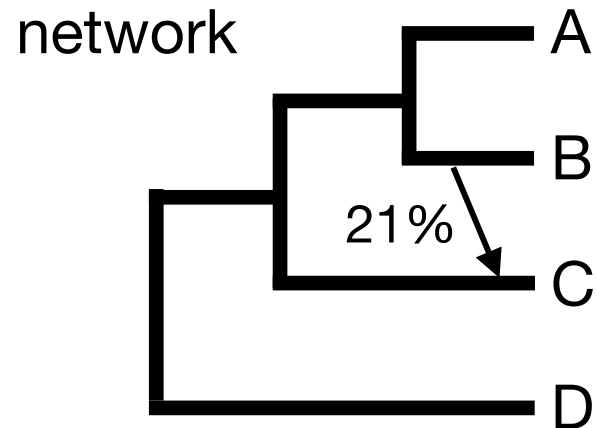
★  $A \rightarrow B$



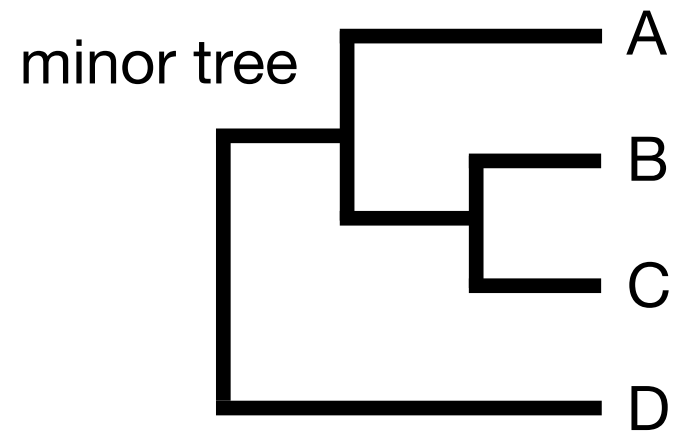




# Major and minor trees

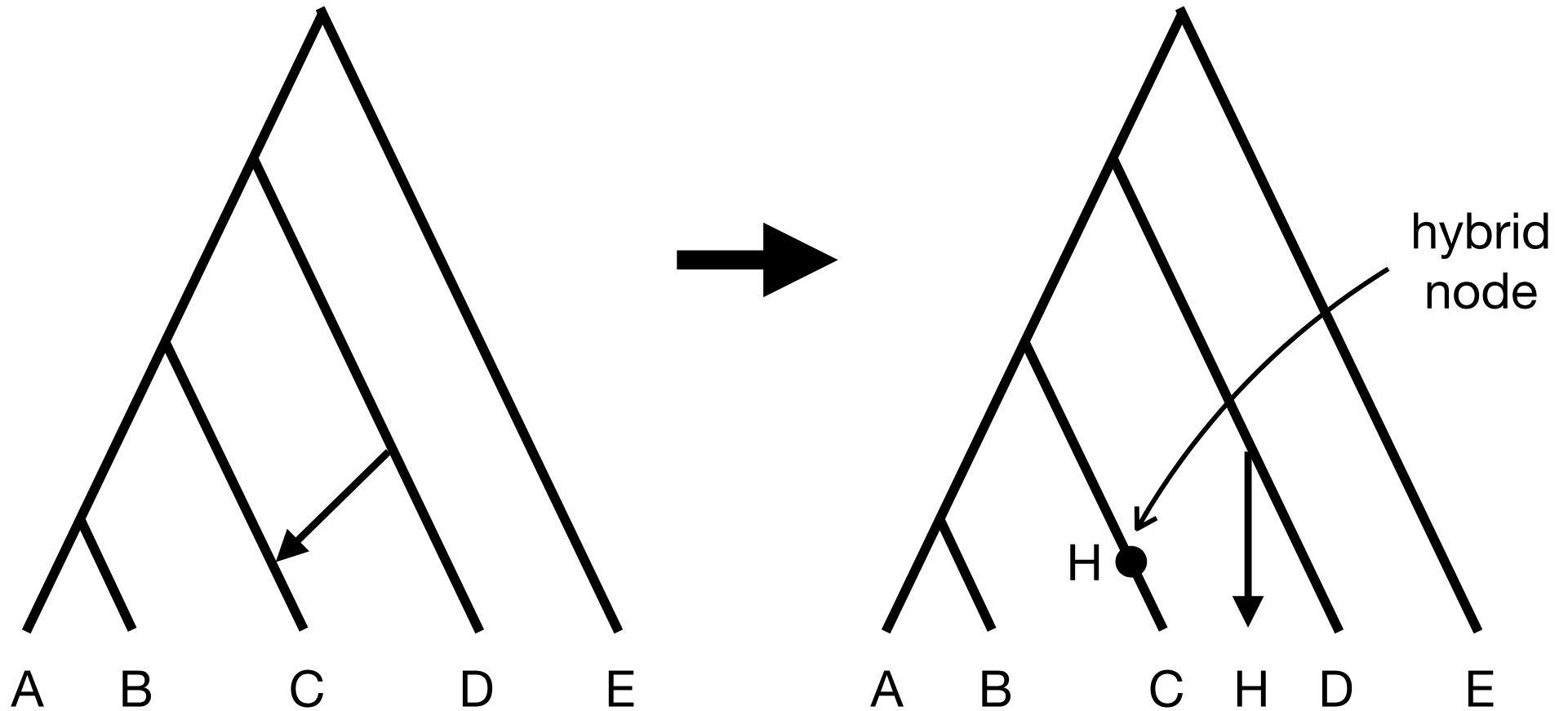


79% of loci



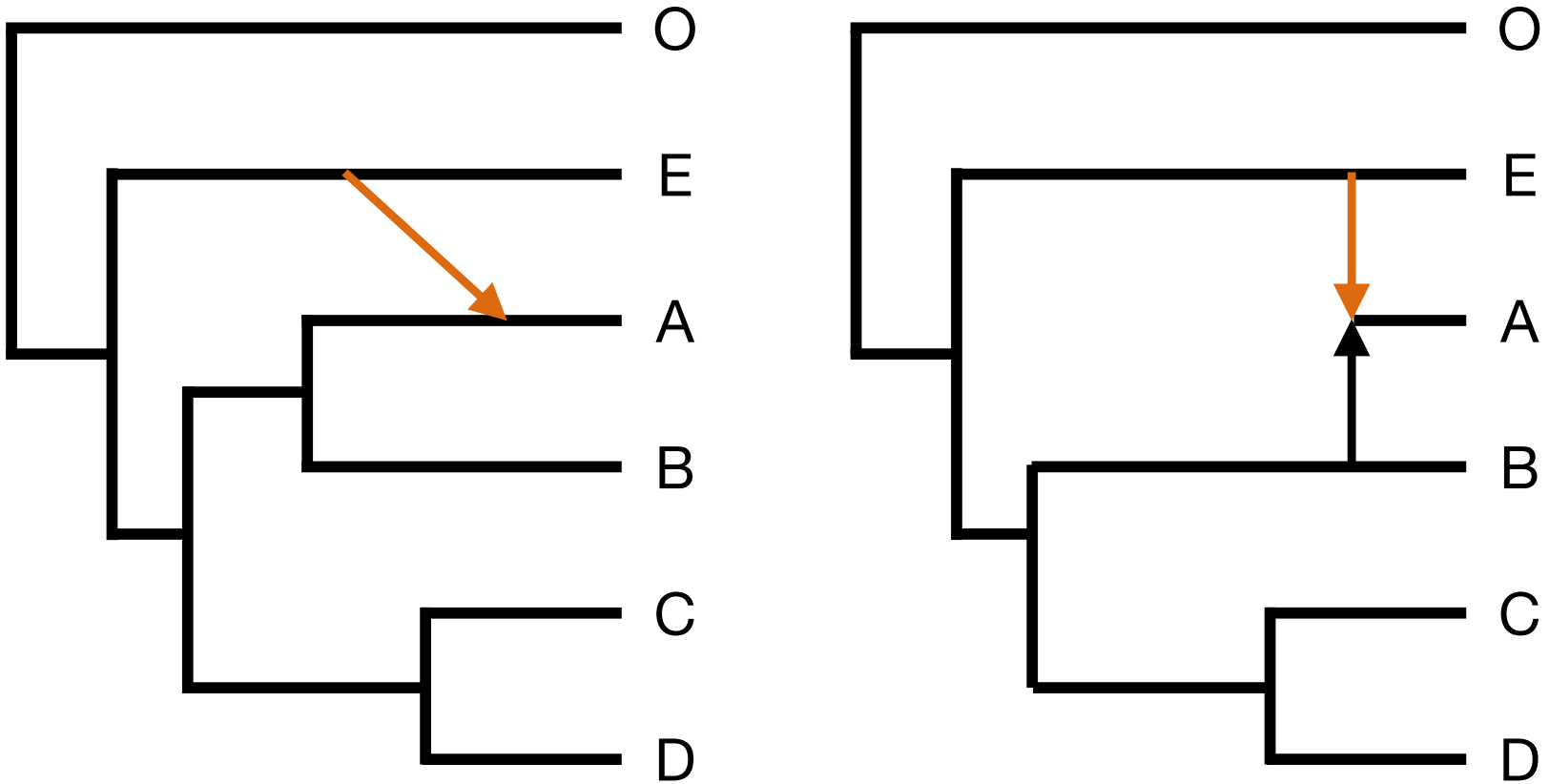
21% of loci

# Network newicks



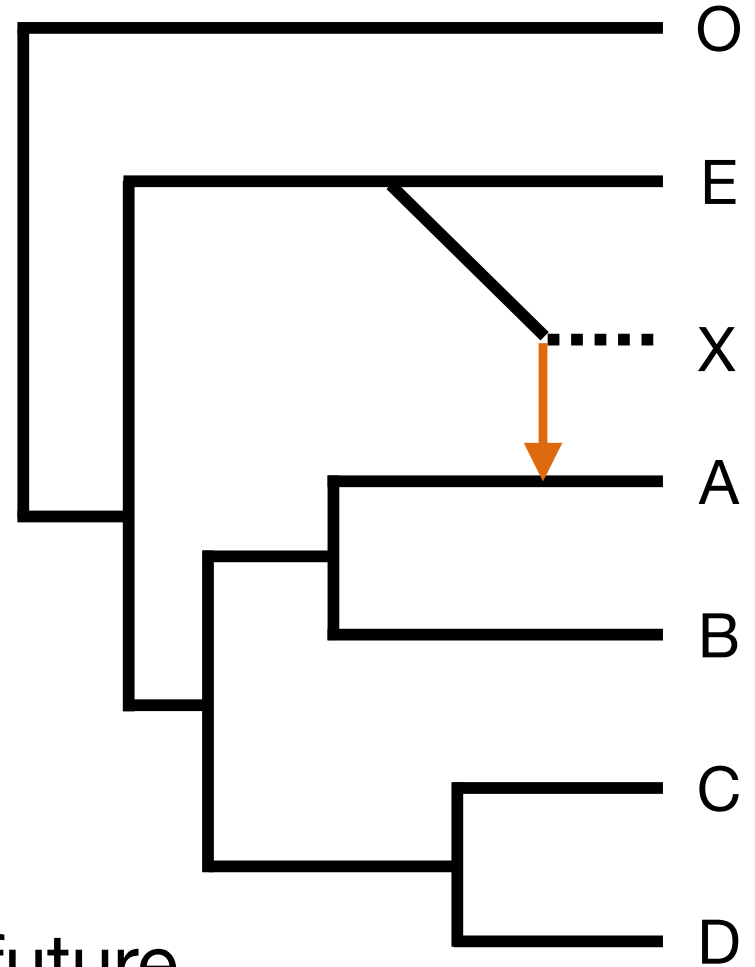
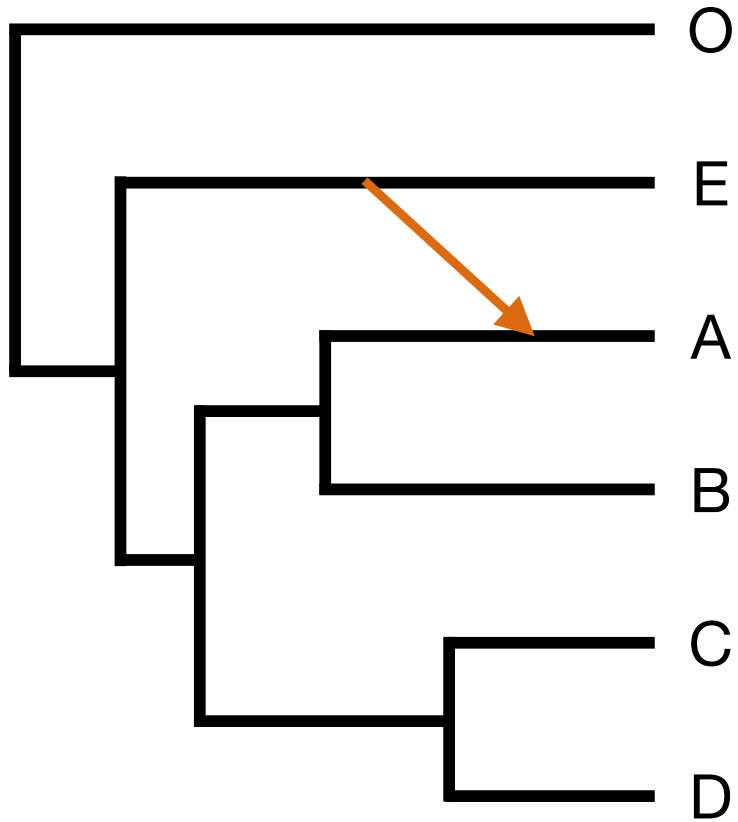
$(((((A,B),(C)\#H),(D,\#H)),E)$

# Artistic license



Same network

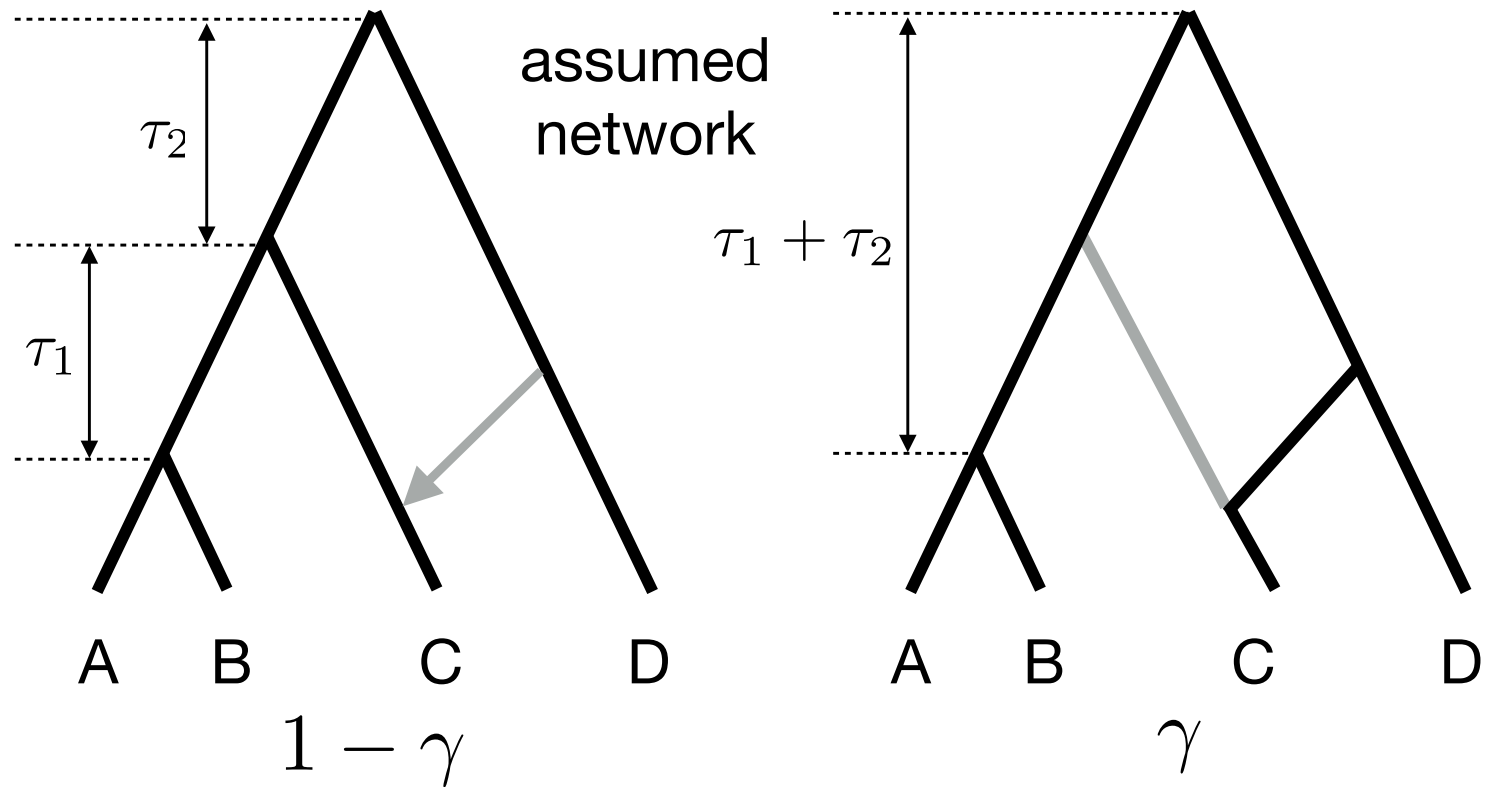
# Ghosts



Gene flow *can* go from past to future

# SNaQ

(Species Networks applying Quartets)



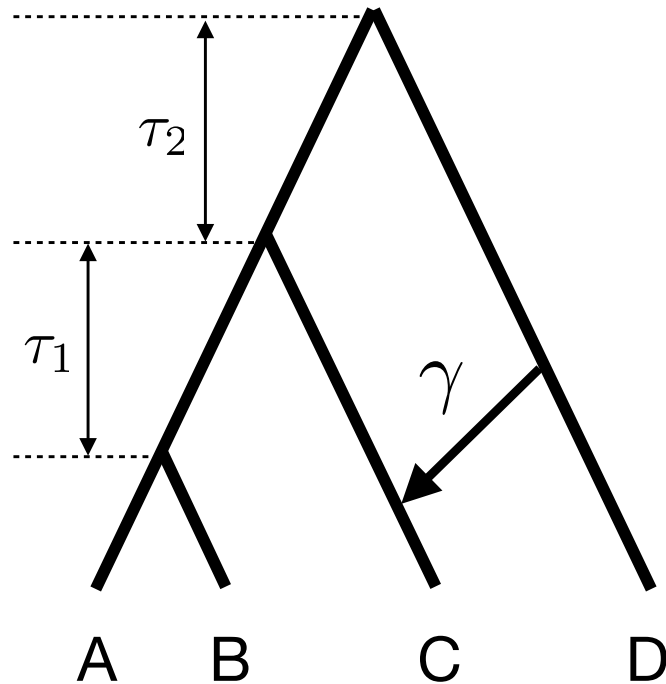
unrooted gene tree probabilities:

$$\Pr(\text{AB}|\text{CD}) = (1 - \gamma) \left(1 - \frac{2}{3}e^{-\tau_1}\right) + \gamma \left(1 - \frac{2}{3}e^{-(\tau_1 + \tau_2)}\right)$$

$$\Pr(\text{AC}|\text{BD}) = (1 - \gamma) \left(\frac{1}{3}e^{-\tau_1}\right) + \gamma \left(\frac{1}{3}e^{-(\tau_1 + \tau_2)}\right)$$

$$\Pr(\text{AD}|\text{BC}) = (1 - \gamma) \left(\frac{1}{3}e^{-\tau_1}\right) + \gamma \left(\frac{1}{3}e^{-(\tau_1 + \tau_2)}\right)$$

# SNaQ



Likelihood of this species network is the multinomial probability of observing:

- $n_1$  gene trees with split AB|CD
- $n_2$  gene trees with split AC|BD
- $n_3$  gene trees with split AD|BC

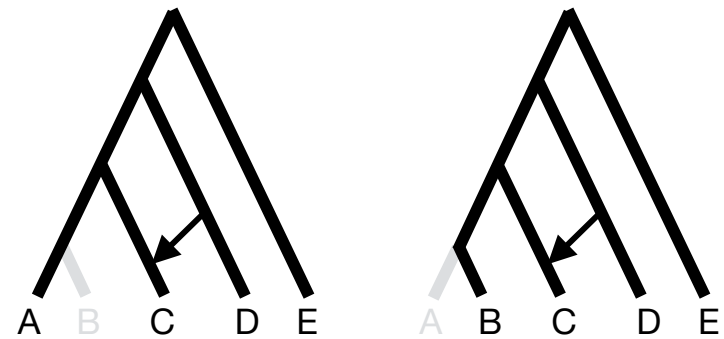
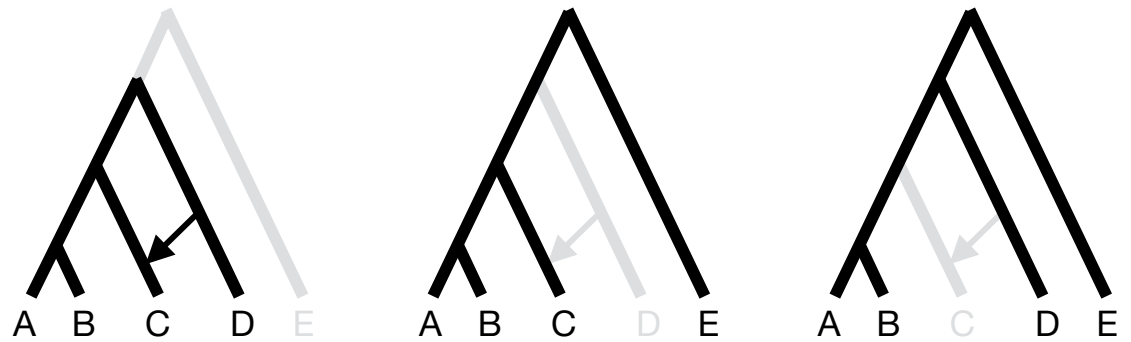
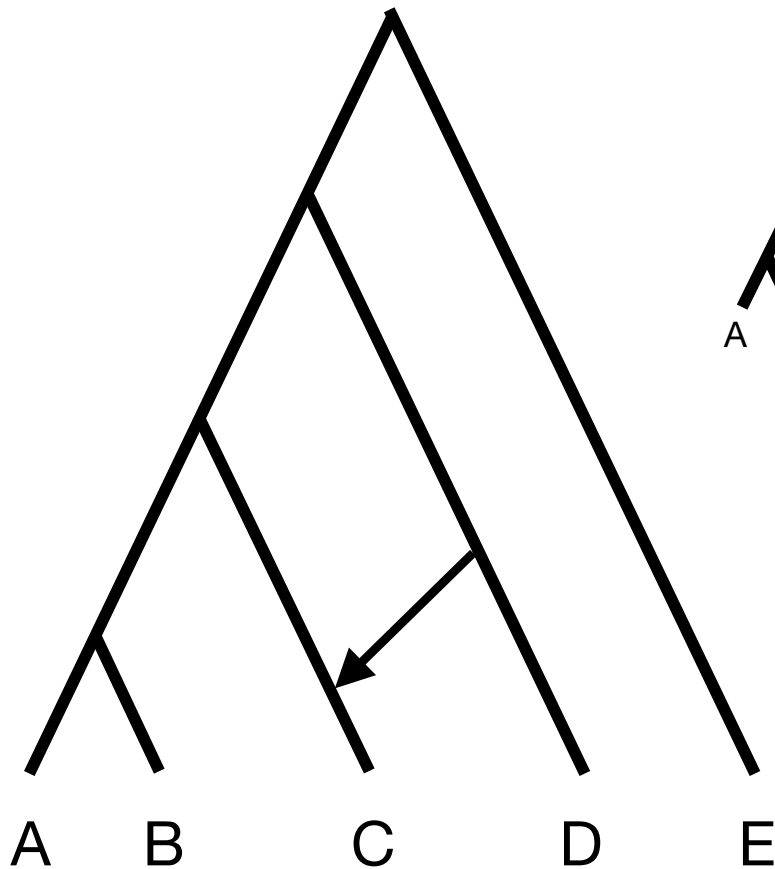
$$L = \Pr(\text{AB|CD})^{n_1} \Pr(\text{AC|BD})^{n_2} \Pr(\text{AD|BC})^{n_3}$$

The probabilities are conditional on the network topology and particular values for  $\tau_1, \tau_2$ , and  $\gamma$ , but my notation omits this.

SNaQ searches through networks,  $\tau$  values, and  $\gamma$  values to find the maximum likelihood species network.

# SNaQ pseudolikelihoods

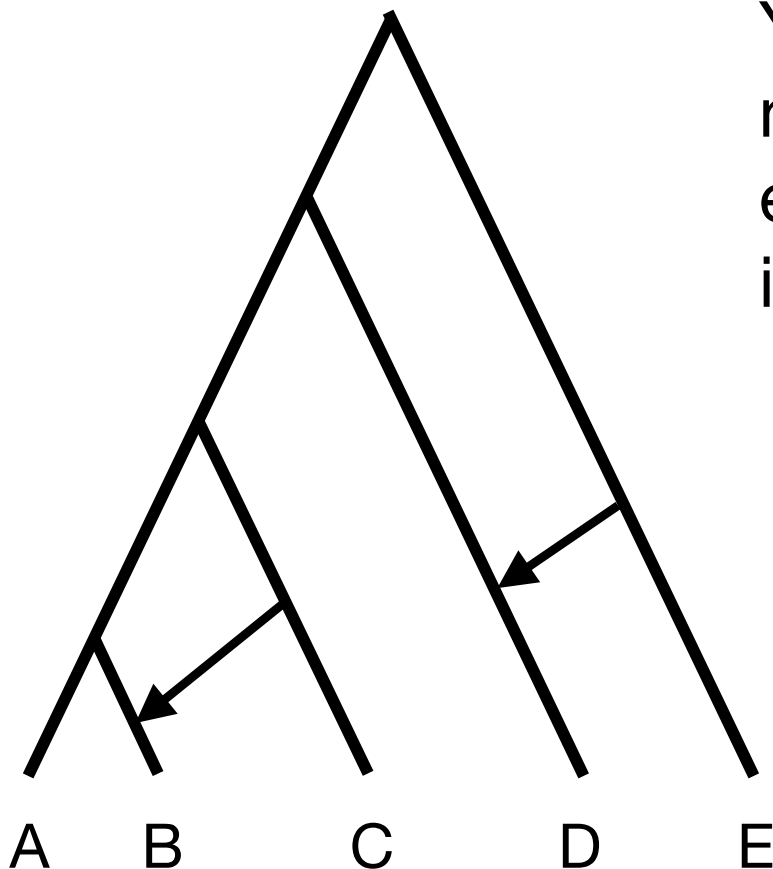
What if there are more than 4 taxa in the network?



Pseudolikelihood is the product of quartet likelihoods.

# SNaQ pseudolikelihoods

What if there is more than one introgression event?

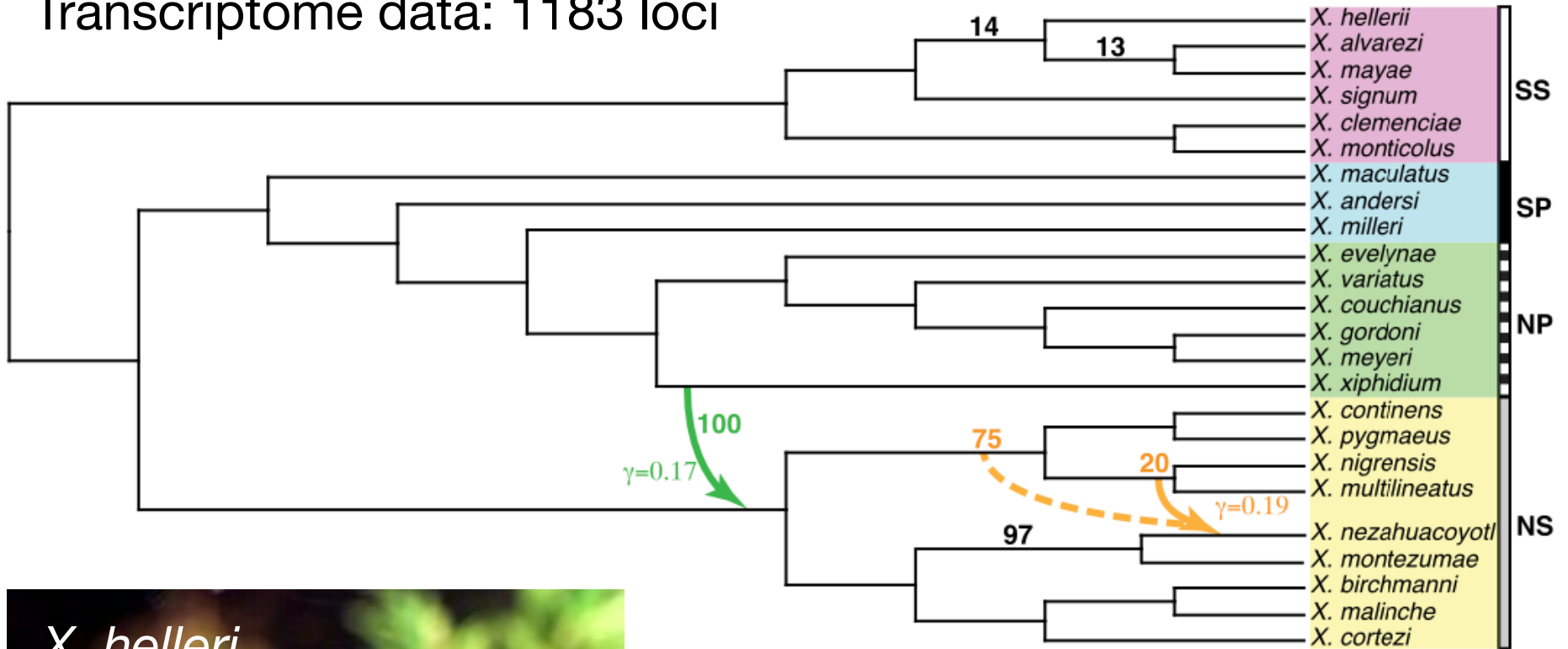


You specify  $k$ , the maximum number of events, and it will estimate networks with 0 to  $k$  introgression events.

Can use AIC/BIC to decide which value of  $k$  provides the best fit.

# *Xiphophorus* fishes

Transcriptome data: 1183 loci



SS (southern swordtails); NS (northern swordtails);  
SP (southern platyfishes); NP (northern platyfishes)

# Network Software

**SNaQ**     <https://github.com/JuliaPhylo/PhyloNetworks.jl>  
<https://github.com/solislemuslab/snaq-tutorial>

**BEAST2**     <https://www.beast2.org>

**PhyloNet**     <https://phylogenomics.rice.edu>

NANUQ, RF-Net, PhyNEST, HyDe, MSCQuartets,...

# Implicit networks

SplitsTree looks like a network, but is really just a way to visualize conflicting splits

