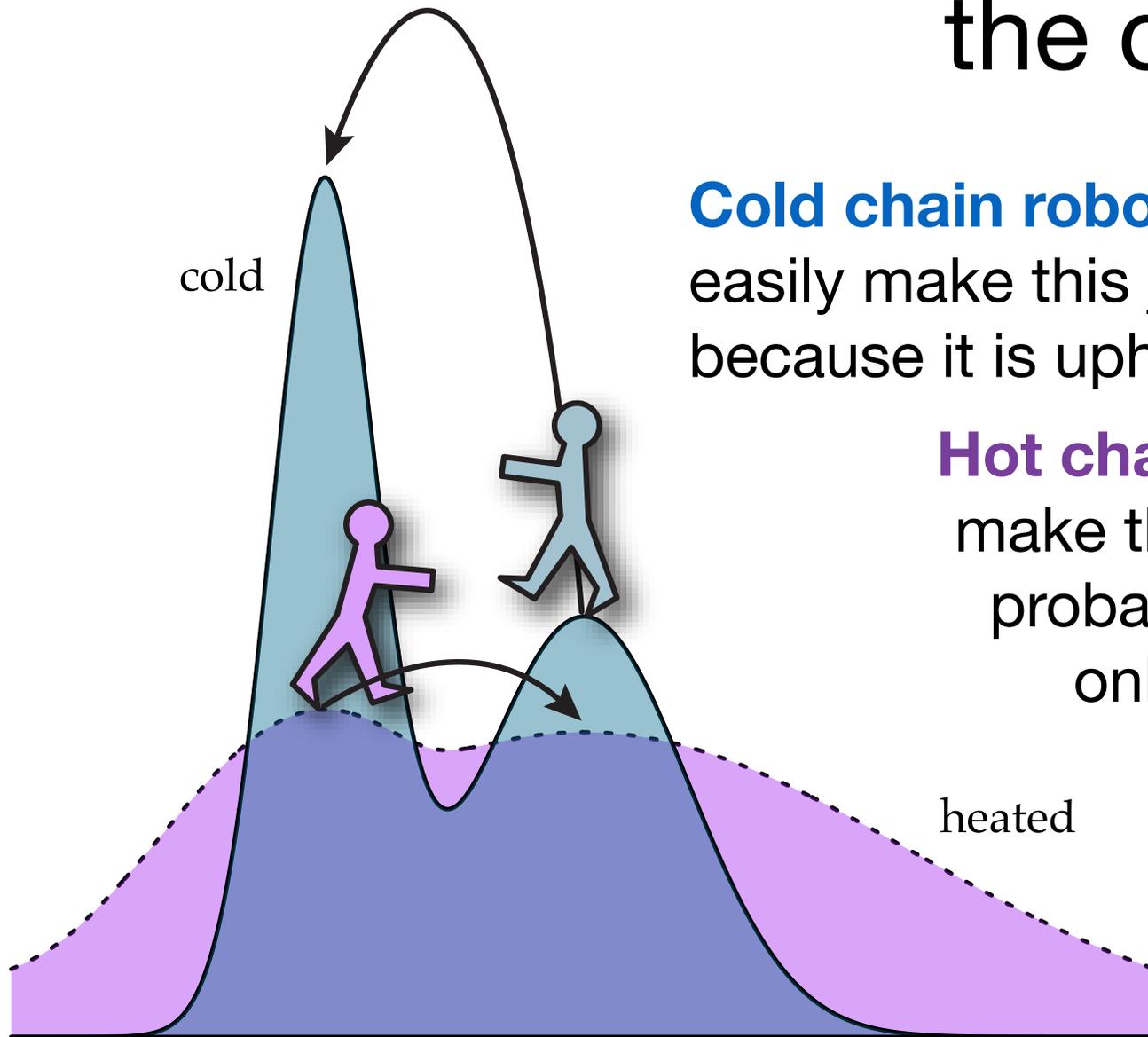


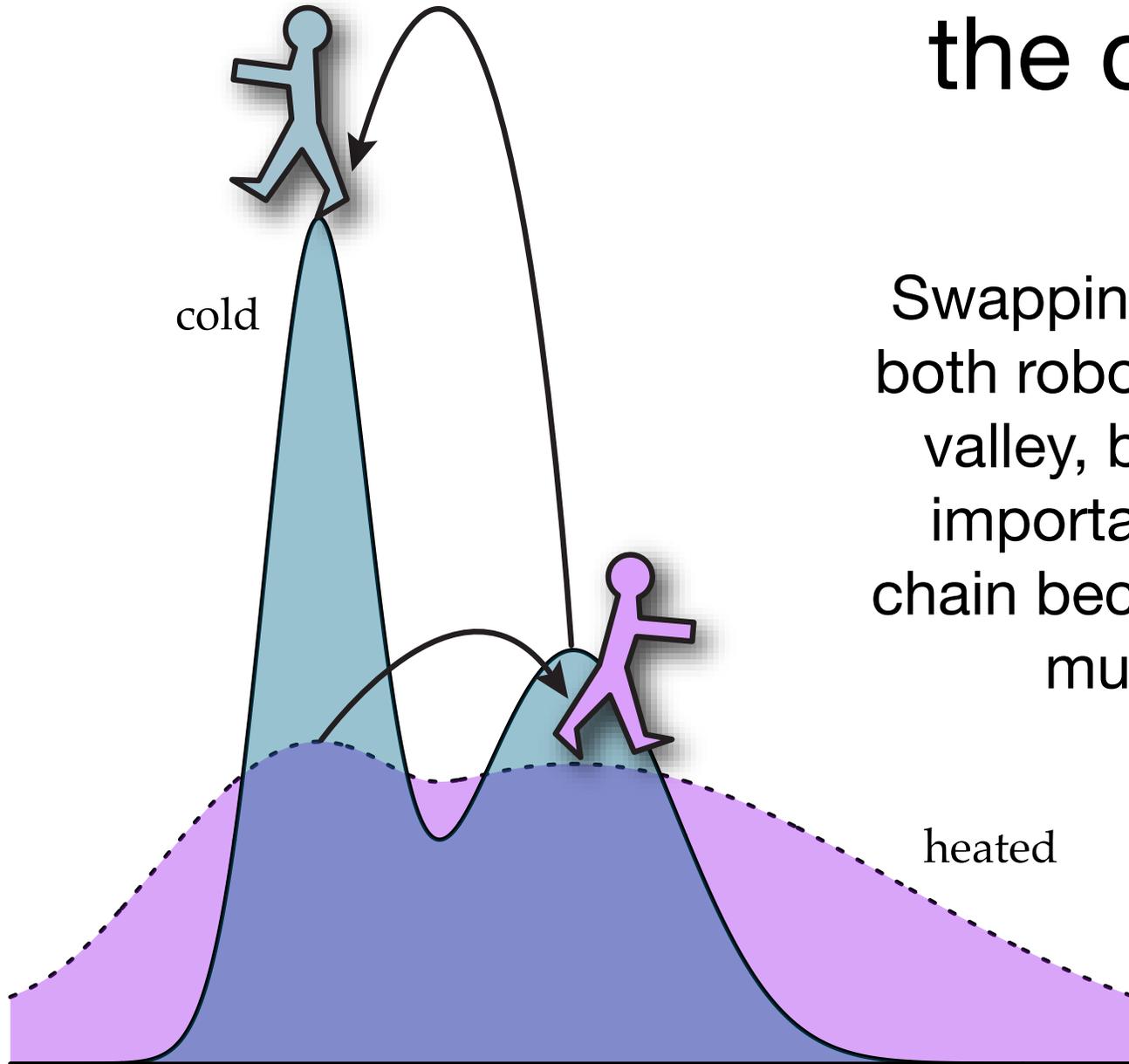
# Heated chains act as scouts for the cold chain



**Cold chain robot** can easily make this jump because it is uphill

**Hot chain robot** can also make this jump with high probability because it is only slightly downhill

# Heated chains act as scouts for the cold chain

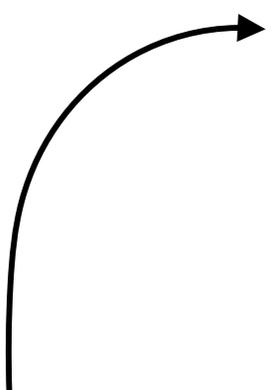


Swapping places means both robots can cross the valley, but this is more important for the cold chain because its valley is much deeper

# Metropolis Algorithm

$$\min \left\{ \frac{p(D|\theta^*) p(\theta^*)}{p(D|\theta) p(\theta)}, 1 \right\}$$

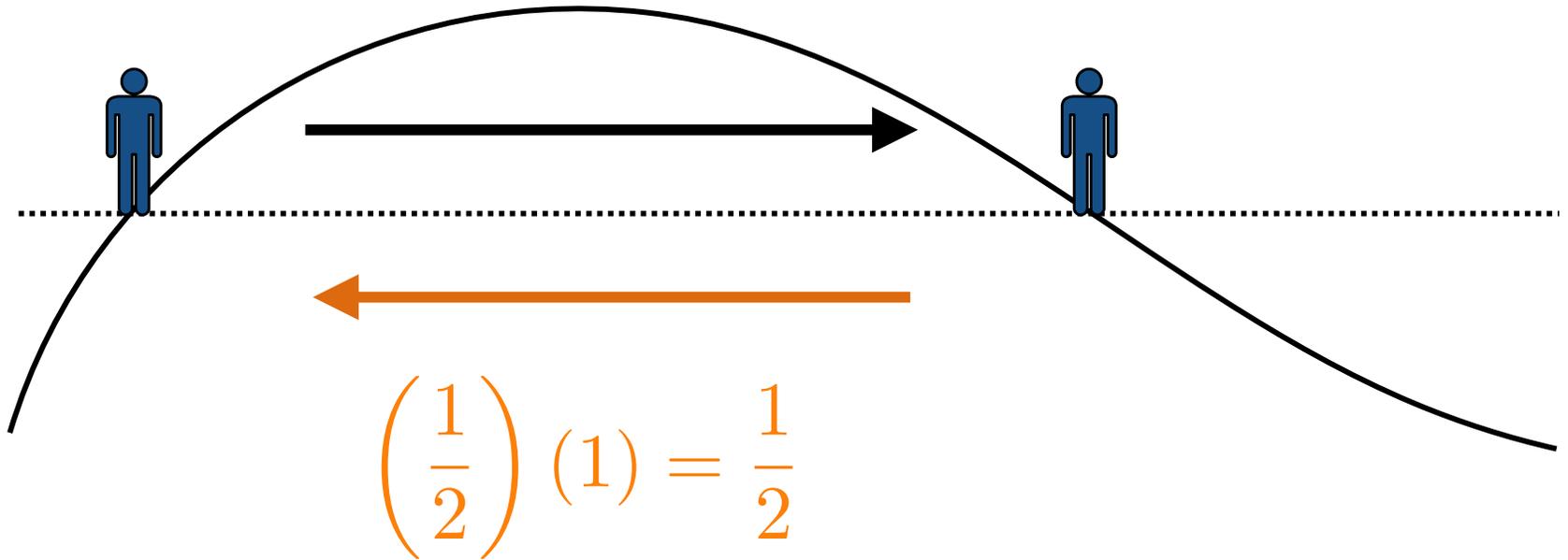
posterior ratio ( $R$ )



Probability of  
accepting the  
proposed move

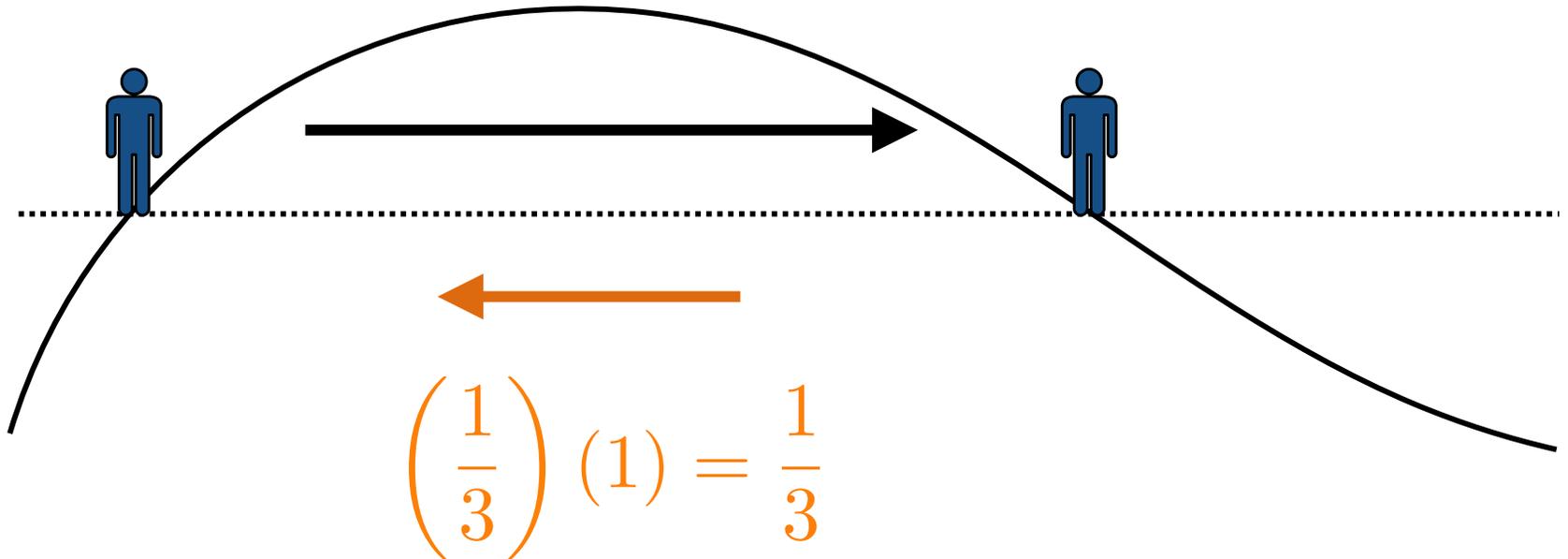
# Hastings ratio

$$\binom{1}{\frac{1}{2}} (1) = \frac{1}{2}$$



# Hastings ratio

$$\binom{2}{\frac{2}{3}}(1) = \frac{2}{3}$$

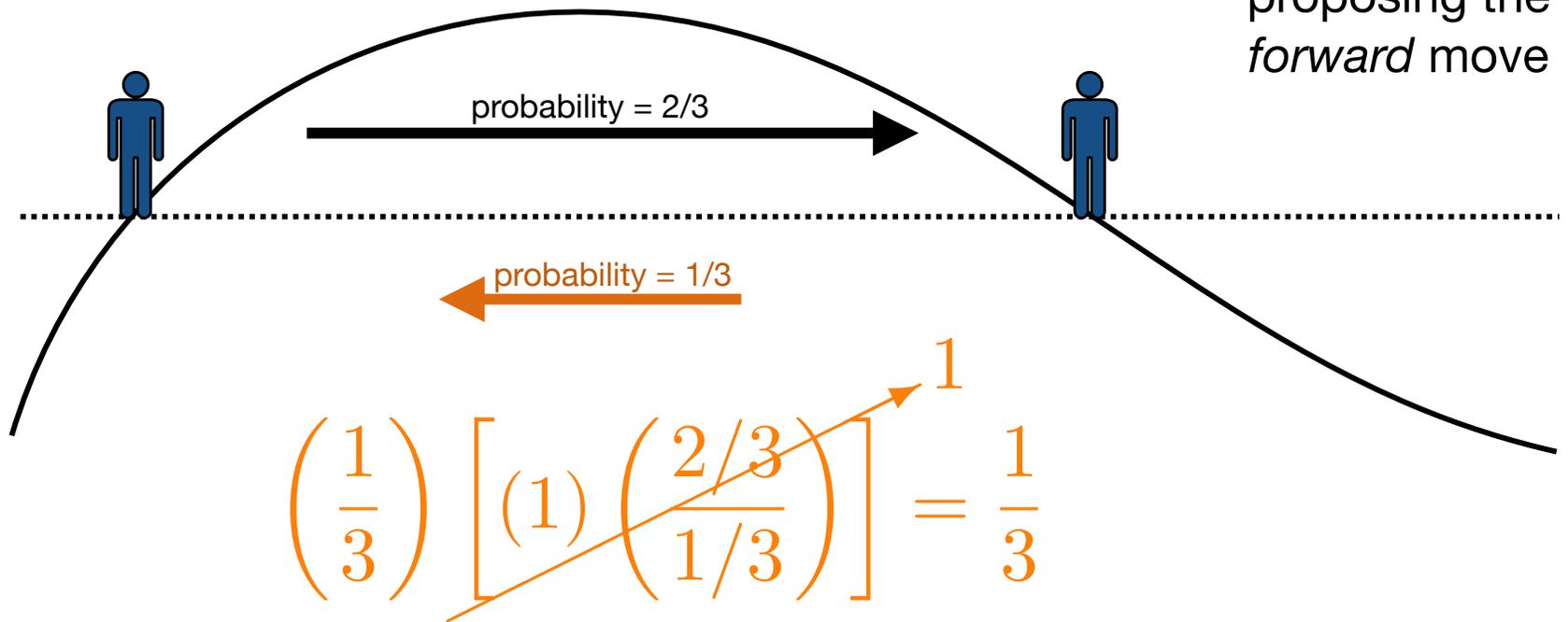


# Hastings ratio

The Hastings ratio is the ratio of the probability of proposing the *reverse* move to the probability of proposing the *forward* move

$$\begin{pmatrix} 2 \\ 3 \end{pmatrix} \left[ (1) \begin{pmatrix} 1/3 \\ 2/3 \end{pmatrix} \right] = \frac{1}{3}$$

← reverse move  
→ forward move



$$\begin{pmatrix} 1 \\ 3 \end{pmatrix} \left[ (1) \begin{pmatrix} 2/3 \\ 1/3 \end{pmatrix} \right] = \frac{1}{3}$$

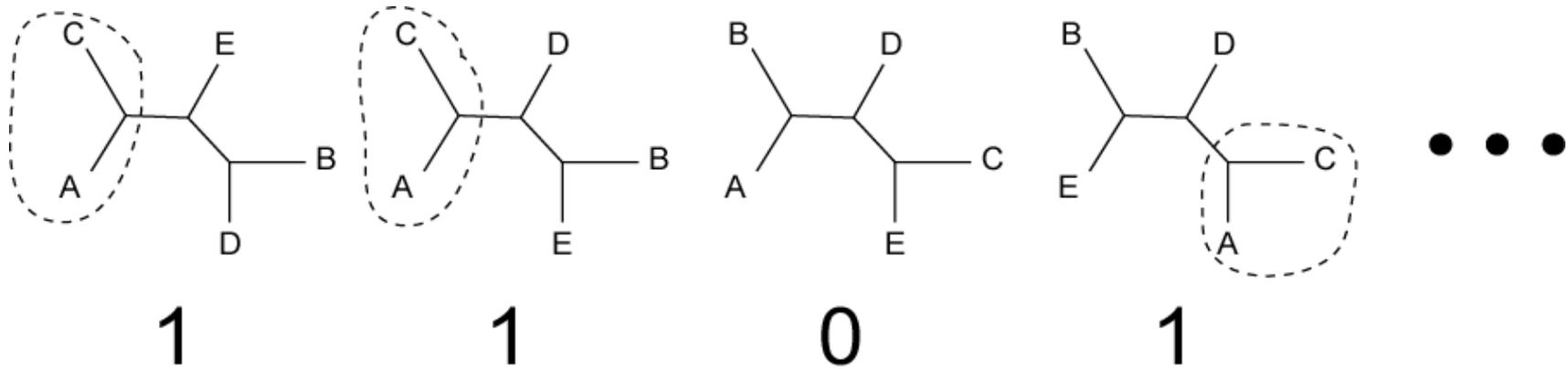
Hastings (1970)

# Metropolis-Hastings Algorithm

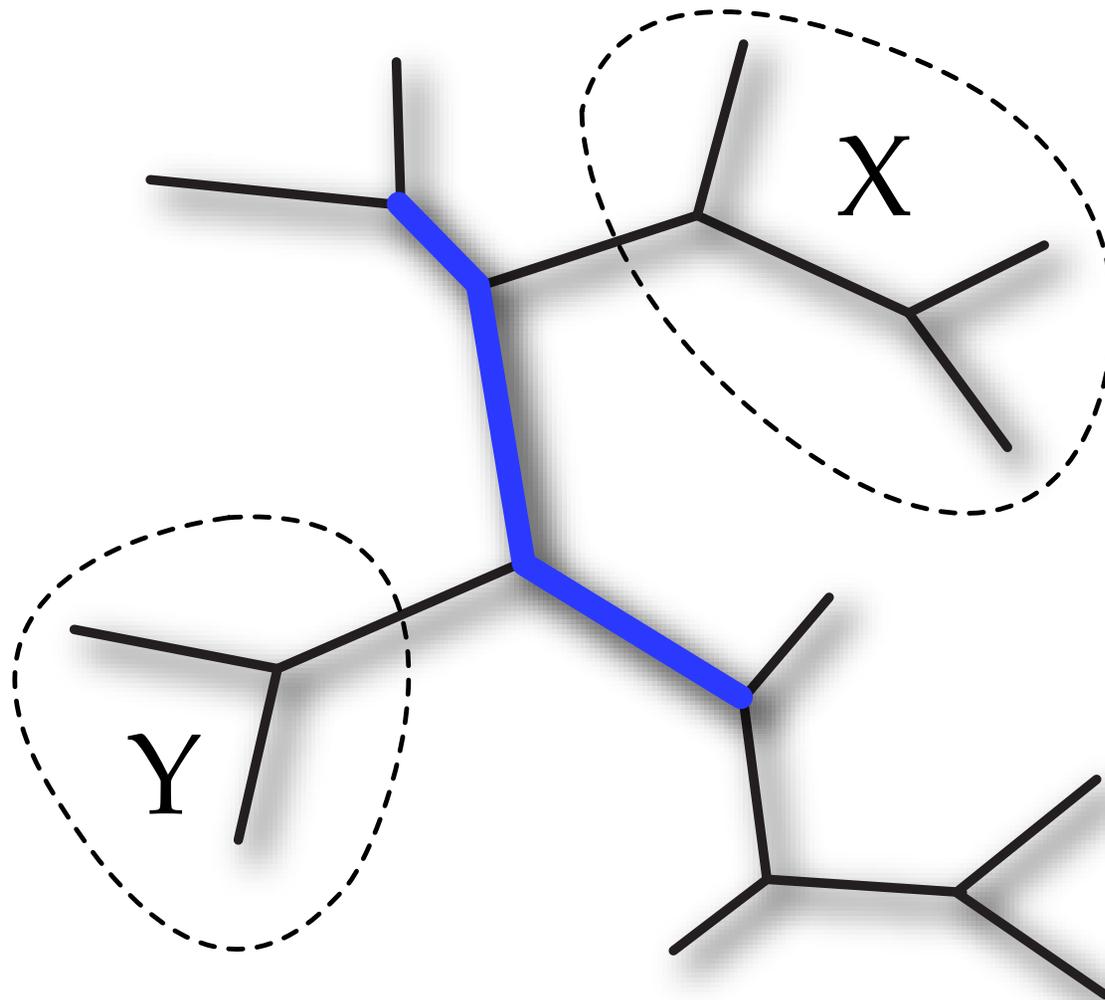
$$\min \left\{ \left[ \frac{p(D|\theta^*) p(\theta^*)}{p(D|\theta) p(\theta)} \right] \left[ \frac{q(\theta|\theta^*)}{q(\theta^*|\theta)} \right], 1 \right\}$$

posterior ratio ( $R$ )                      Hastings ratio

# So, what's all this got to do with phylogenetics?



# Moving through treespace

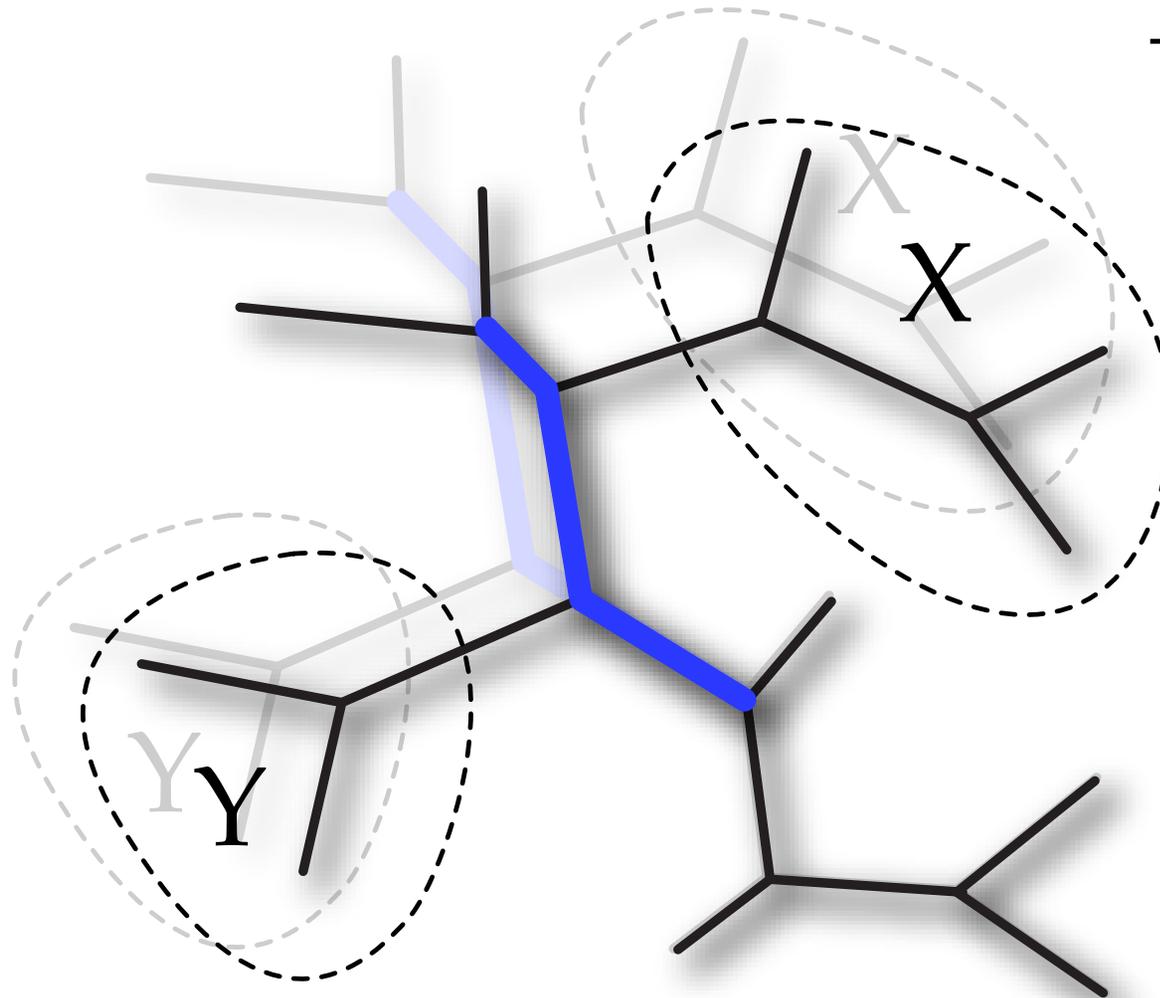


The Target-Simon move

**Step 1:**

Pick 3 contiguous edges randomly, defining two subtrees, X and Y

# Moving through treespace



## The Target-Simon move

### Step 1:

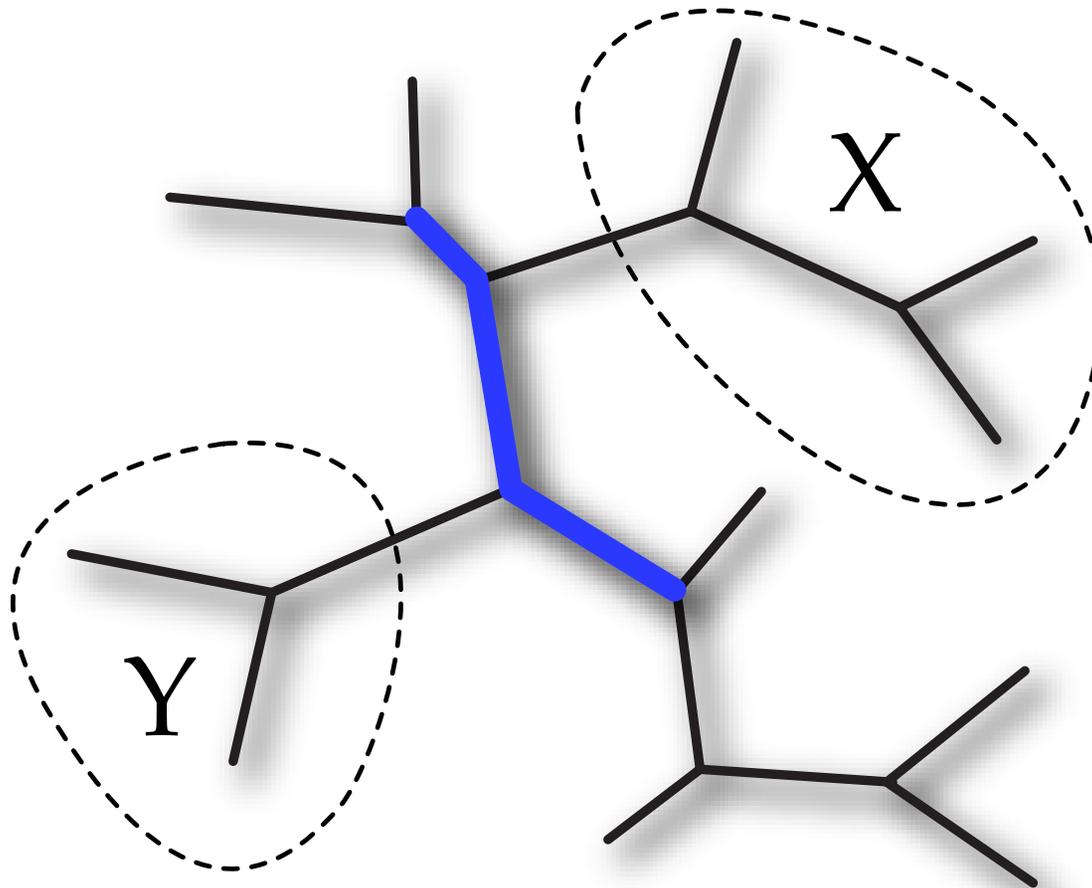
Pick 3 contiguous edges randomly, defining two subtrees, X and Y

### Step 2:

Shrink or grow selected 3-edge segment by a random amount

# Moving through treespace

## The Larget-Simon move



### Step 1:

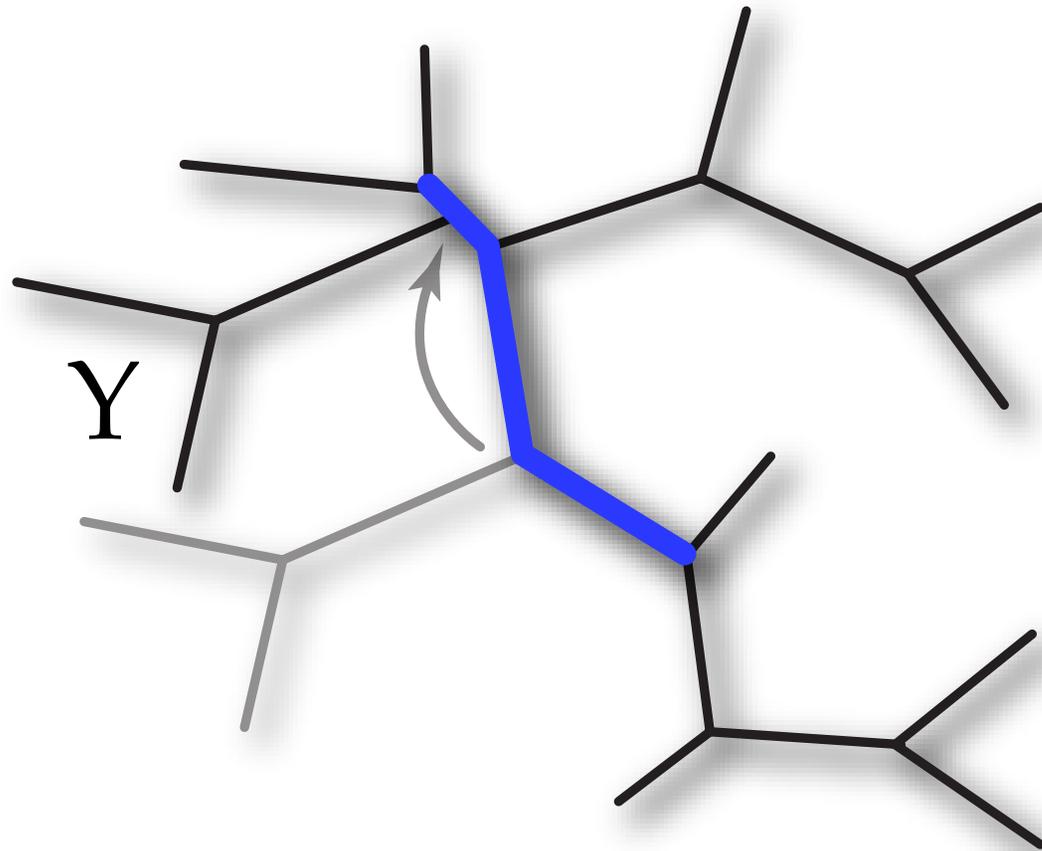
Pick 3 contiguous edges randomly, defining two subtrees, X and Y

### Step 2:

Shrink or grow selected 3-edge segment by a random amount

# Moving through treespace

## The Larget-Simon move



### Step 1:

Pick 3 contiguous edges randomly, defining two subtrees, X and Y

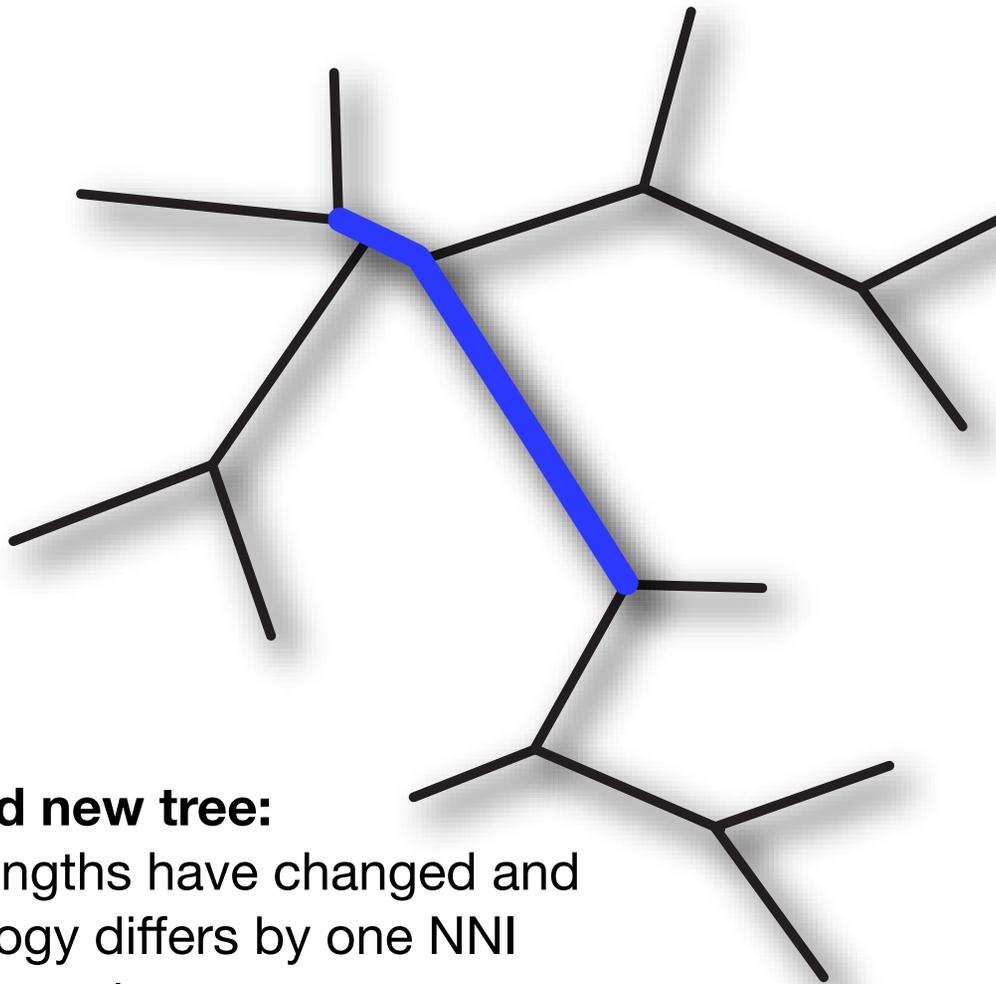
### Step 2:

Shrink or grow selected 3-edge segment by a random amount

### Step 3:

Choose X or Y randomly, then reposition randomly

# Moving through treespace



## Proposed new tree:

3 edge lengths have changed and the topology differs by one NNI rearrangement

## The Larget-Simon move

### Step 1:

Pick 3 contiguous edges randomly, defining two subtrees, X and Y

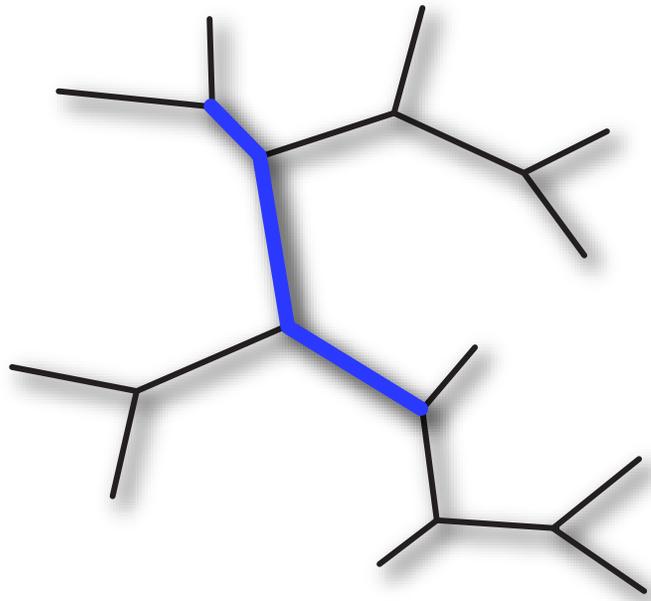
### Step 2:

Shrink or grow selected 3-edge segment by a random amount

### Step 3:

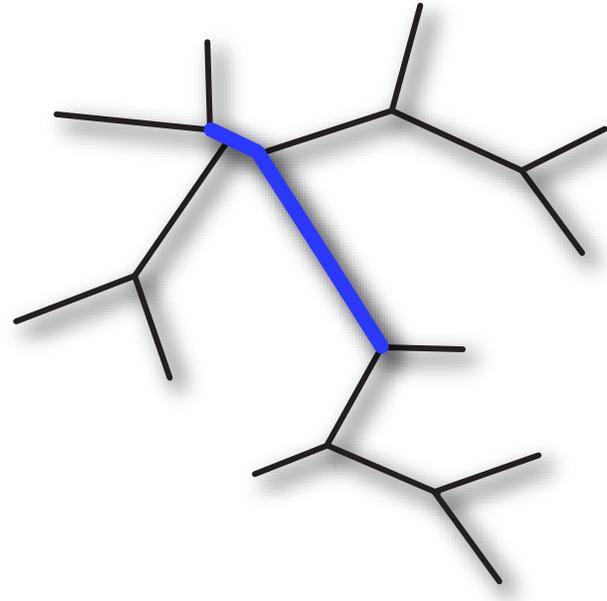
Choose X or Y randomly, then reposition randomly

# Moving through treespace



Current tree

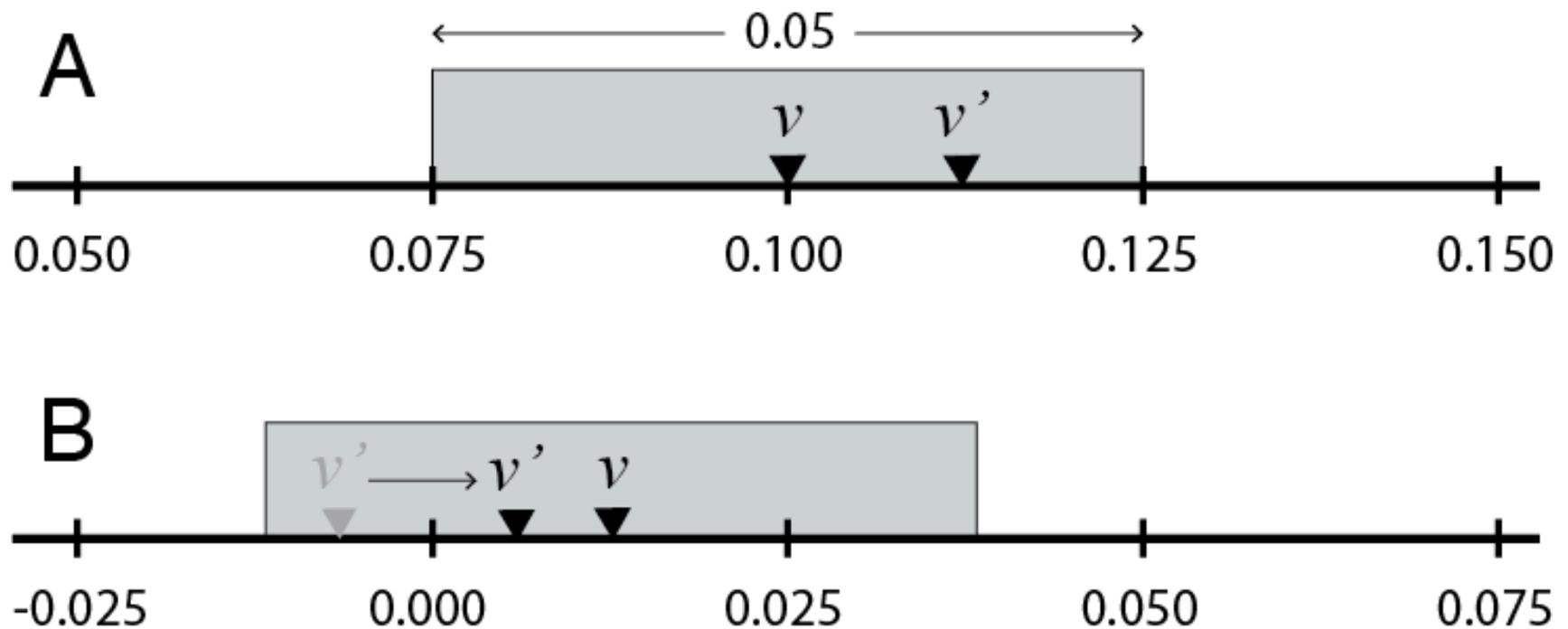
log-posterior = -34256



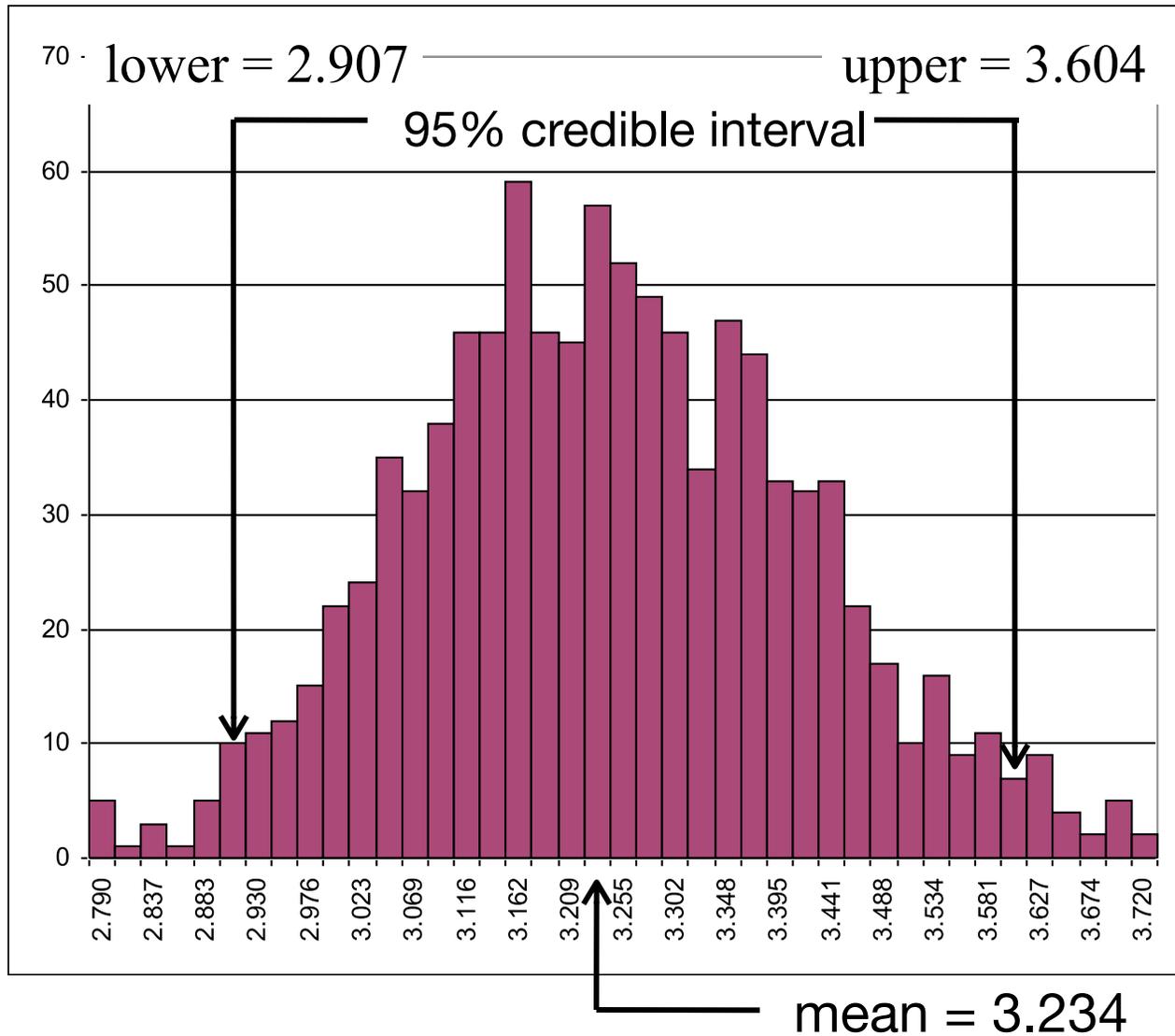
Proposed tree

log-posterior = -32519  
(better, so accept)

# Proposing a new value of a model parameter



# Marginal Posterior Distribution of $\kappa$



Histogram created from a sample of 1000 kappa values.

# Kernel Density Estimation

Estimate density function using  
sampled points

