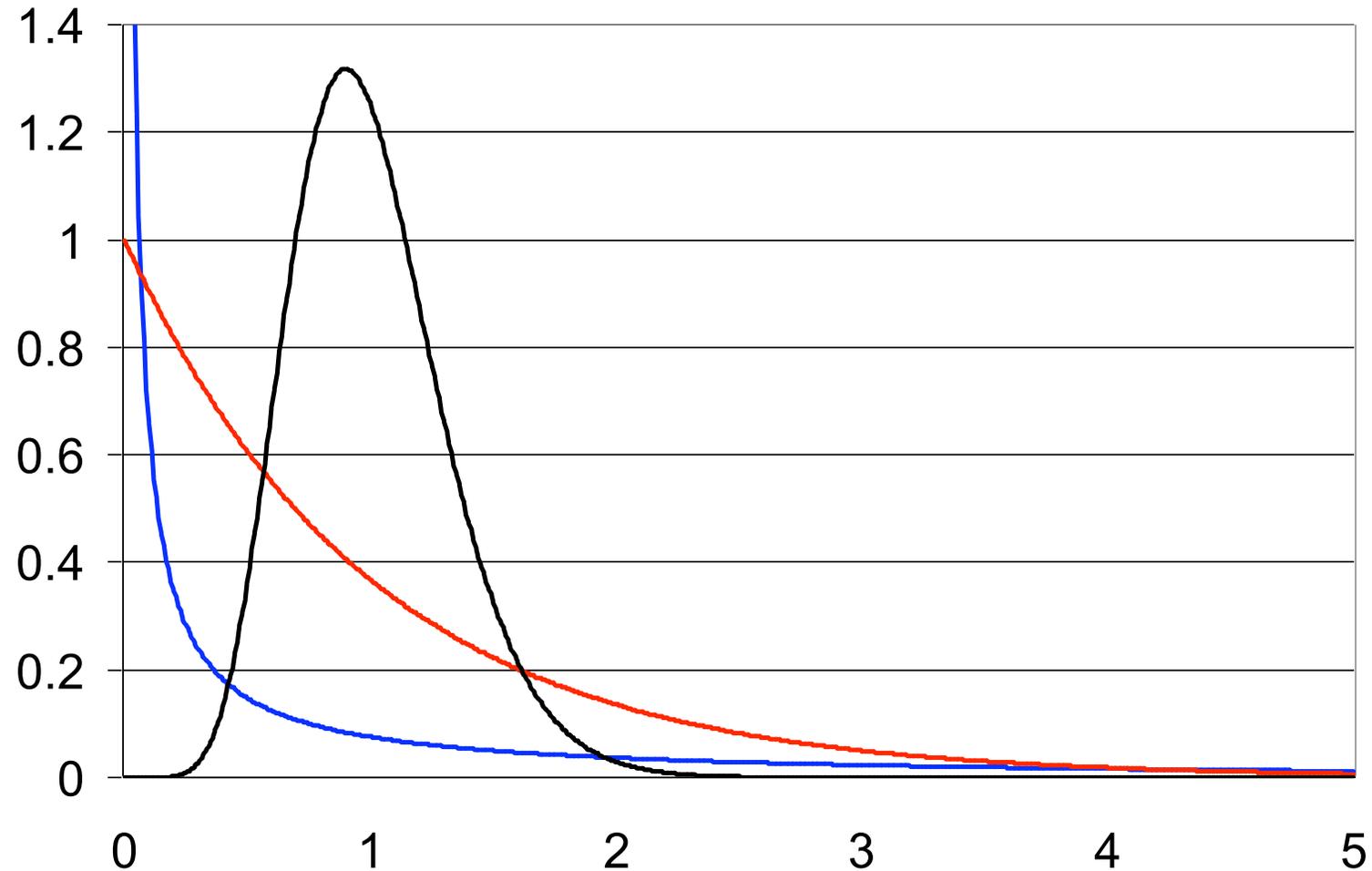
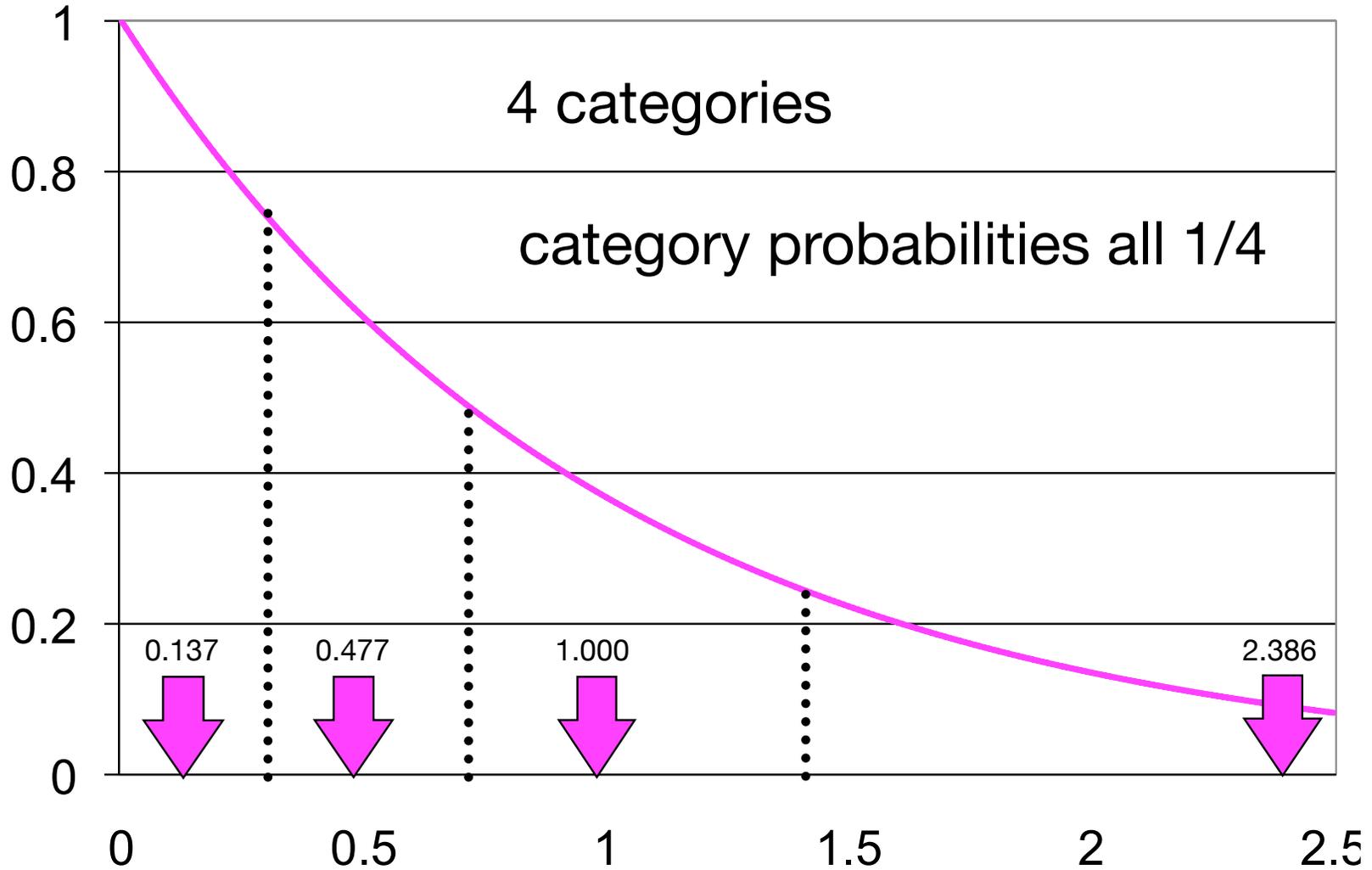


# Discrete Gamma (G) model

# Gamma distributions



# Discrete Gamma (+G)

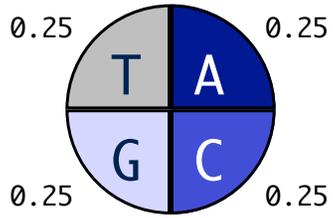


# Free rates (+R)

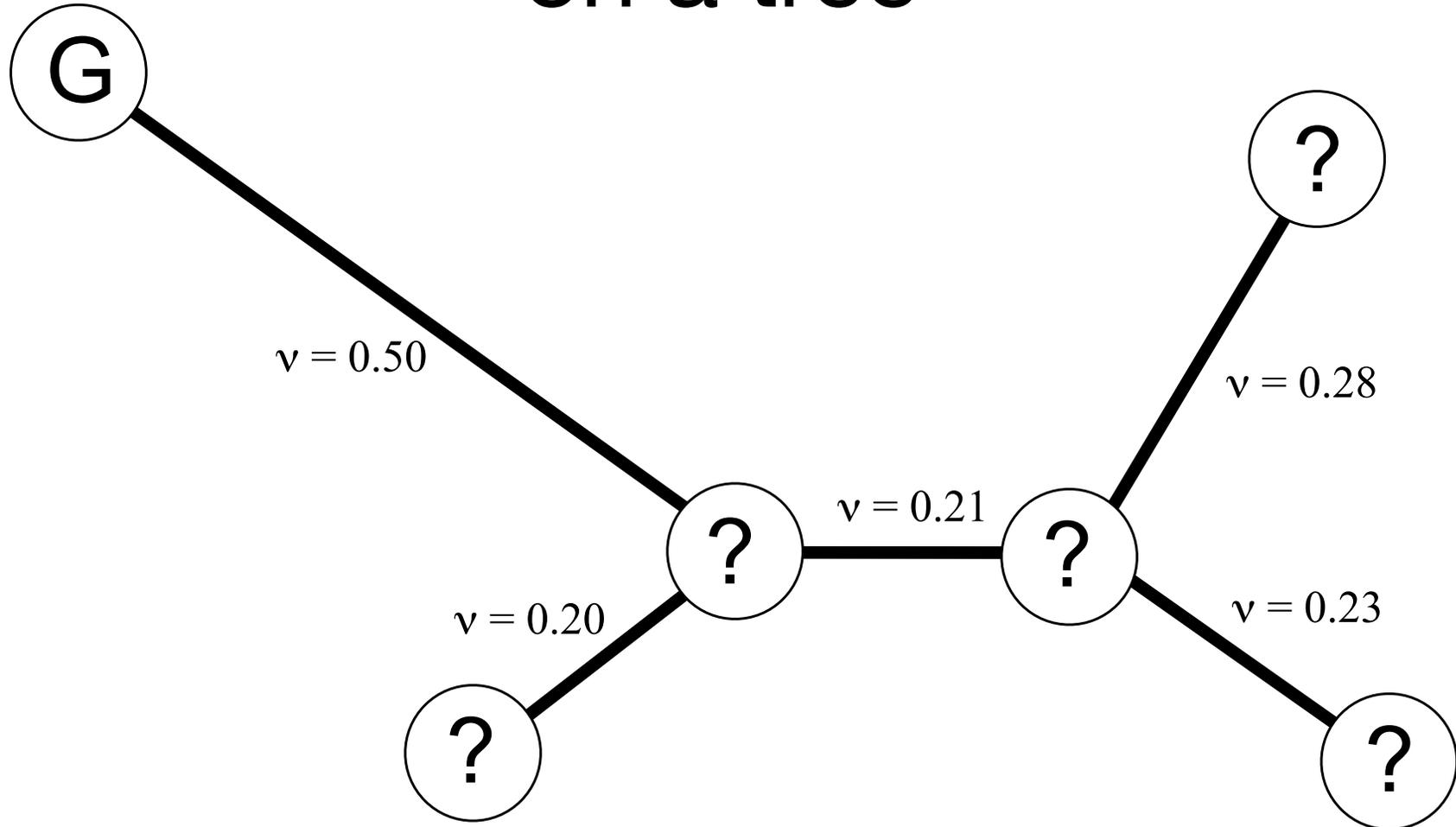
category	relative rates	category probabilities
1	$r_1$	$p_1$
2	$r_2$	$p_2$
3	$r_3$	$p_3$
4	$r_4$	$p_4$

$$p_1 + p_2 + p_3 + p_4 = 1$$

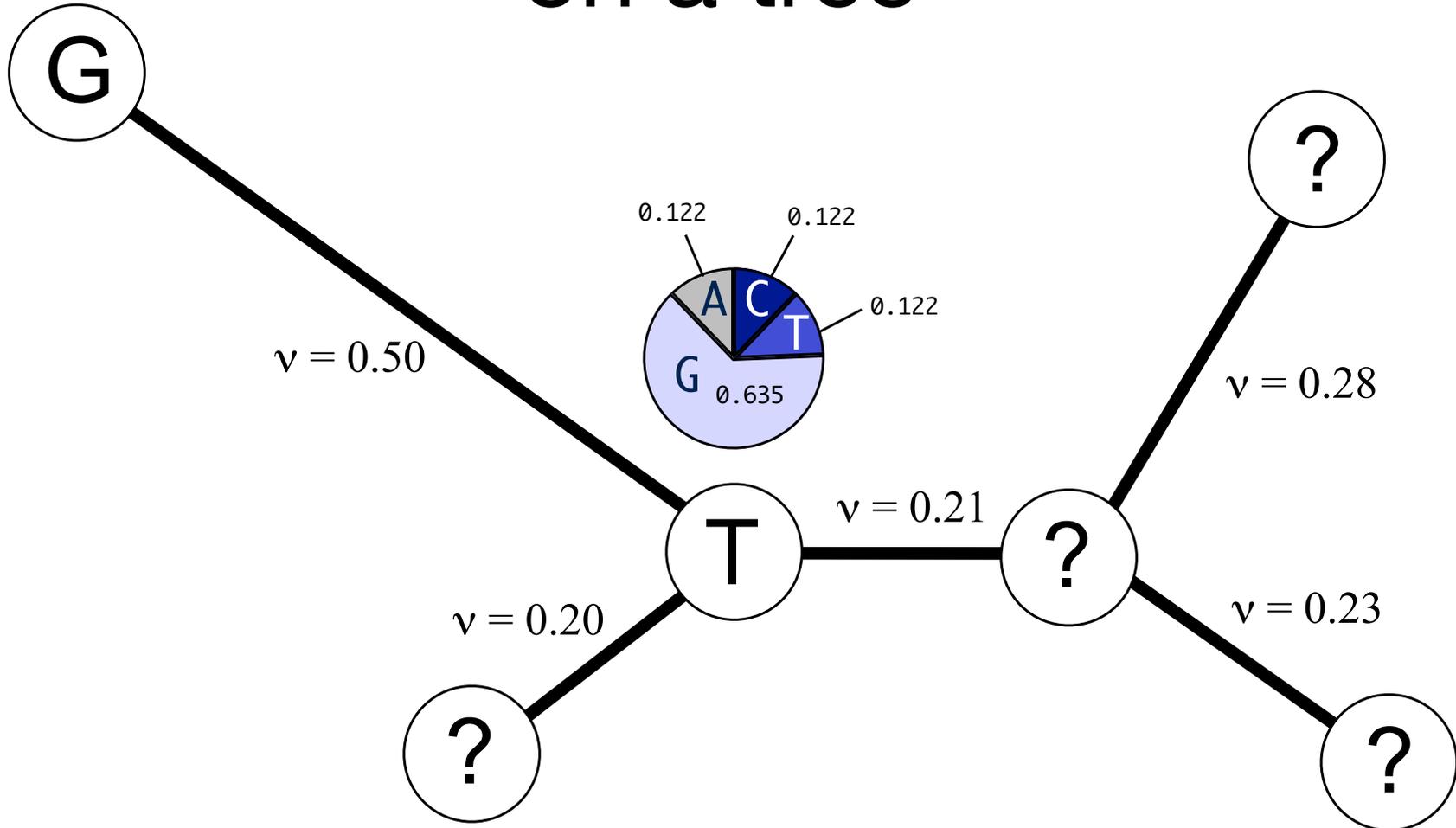
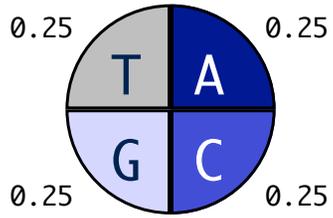
$$p_1 r_1 + p_2 r_2 + p_3 r_3 + p_4 r_4 = 1$$



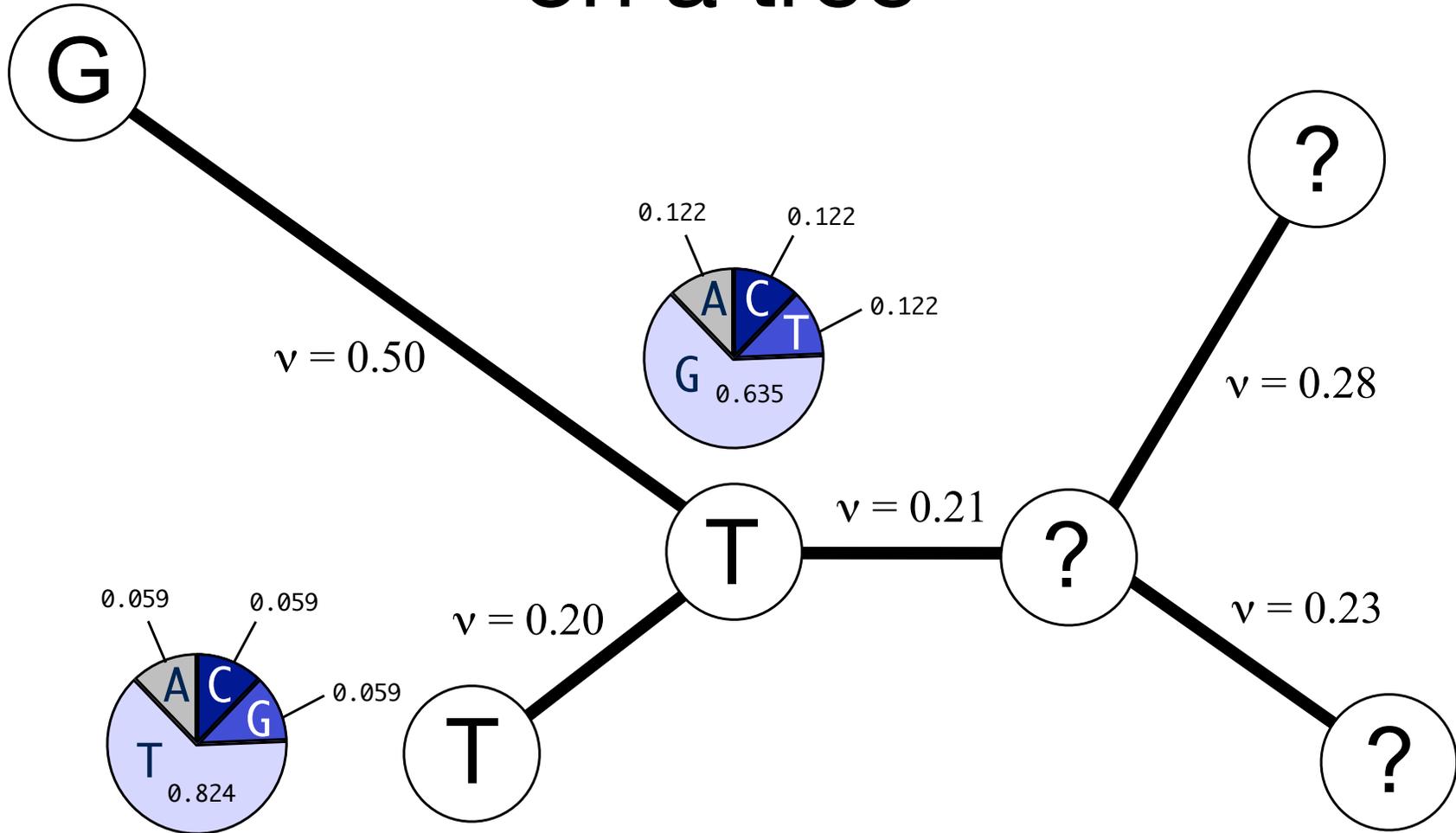
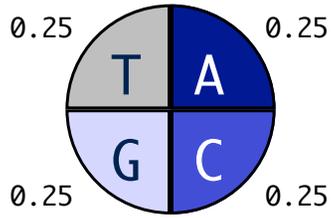
# Simulating a site on a tree



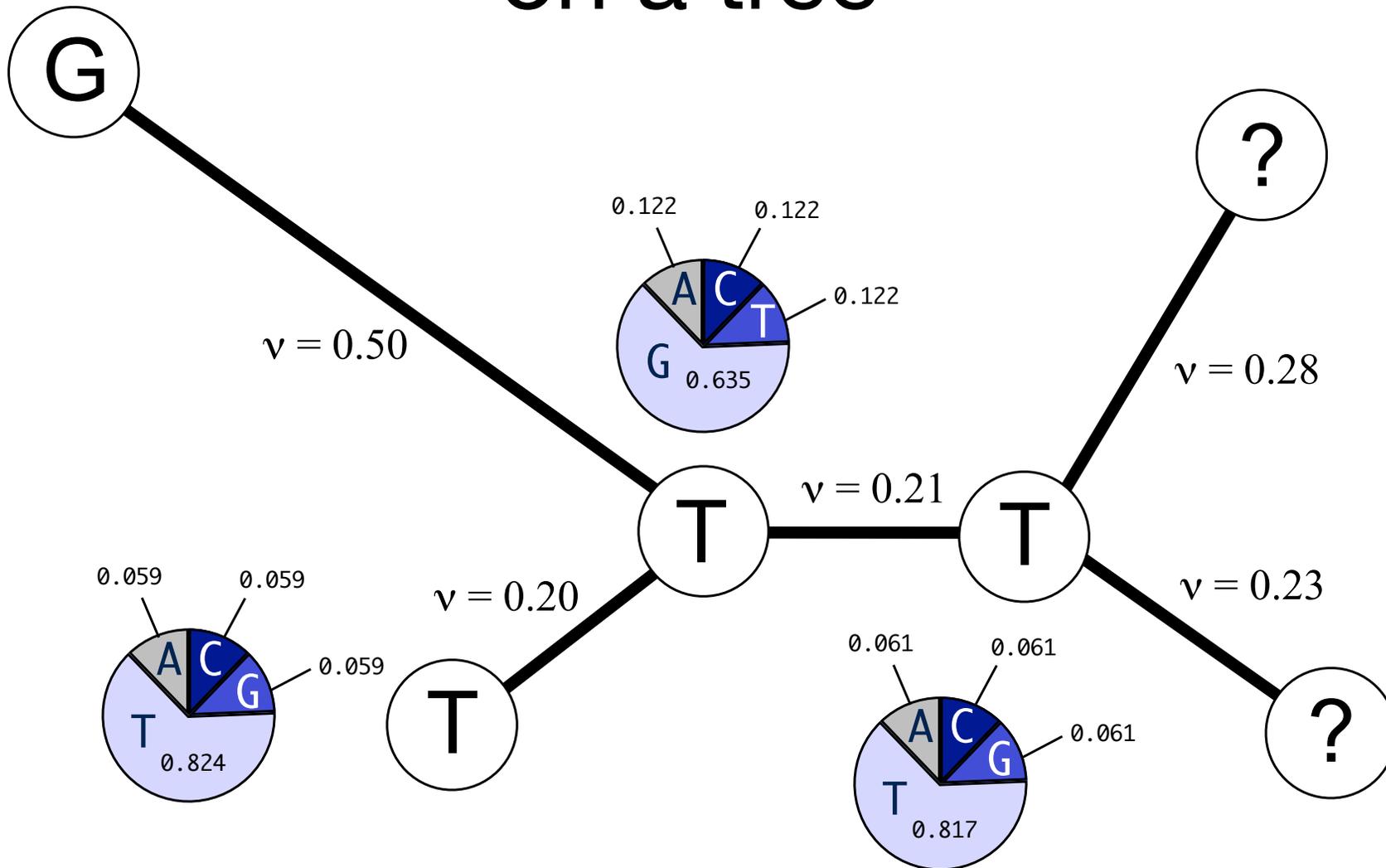
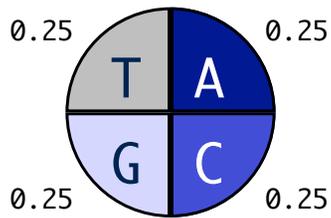
# Simulating a site on a tree



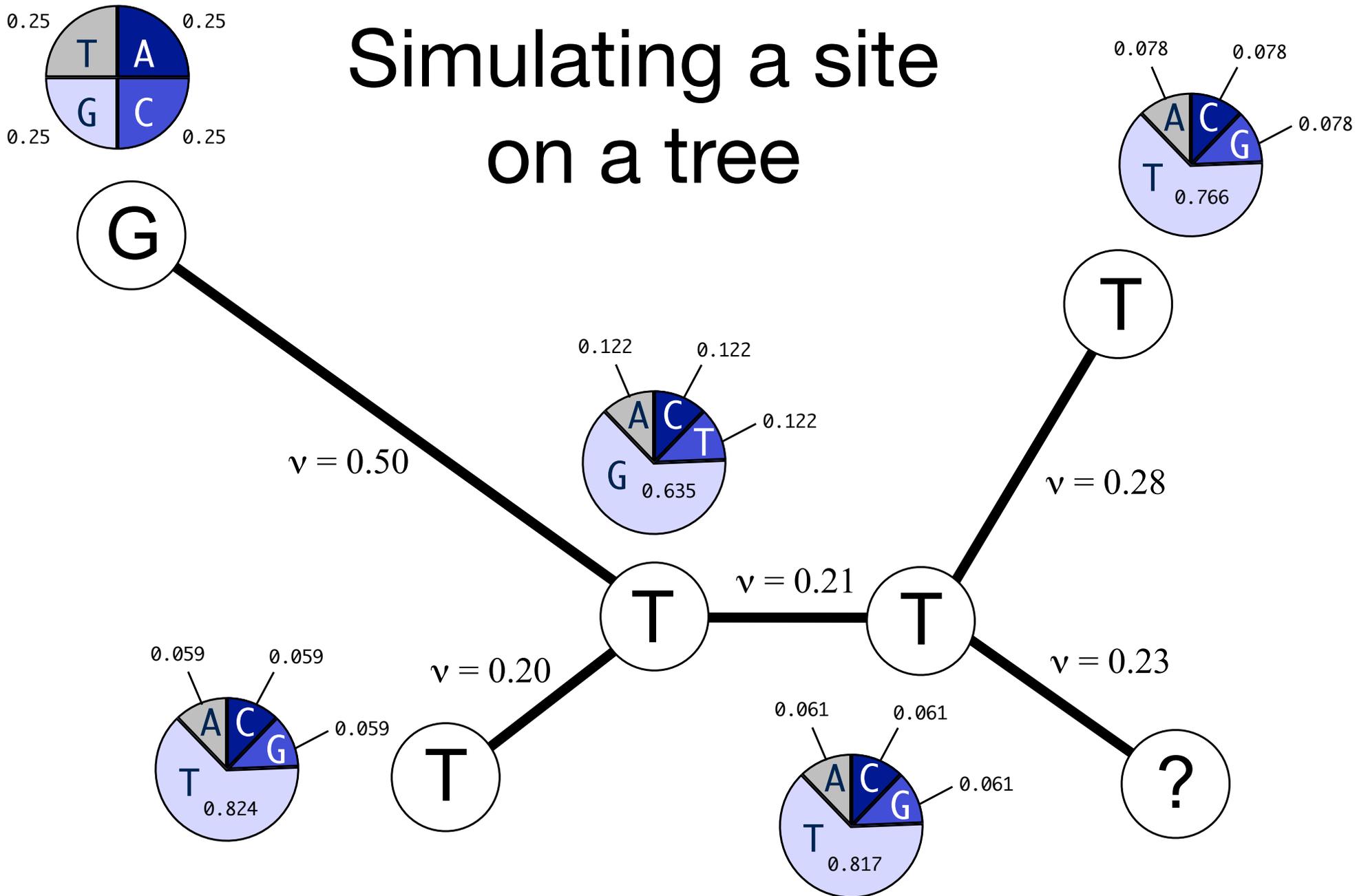
# Simulating a site on a tree



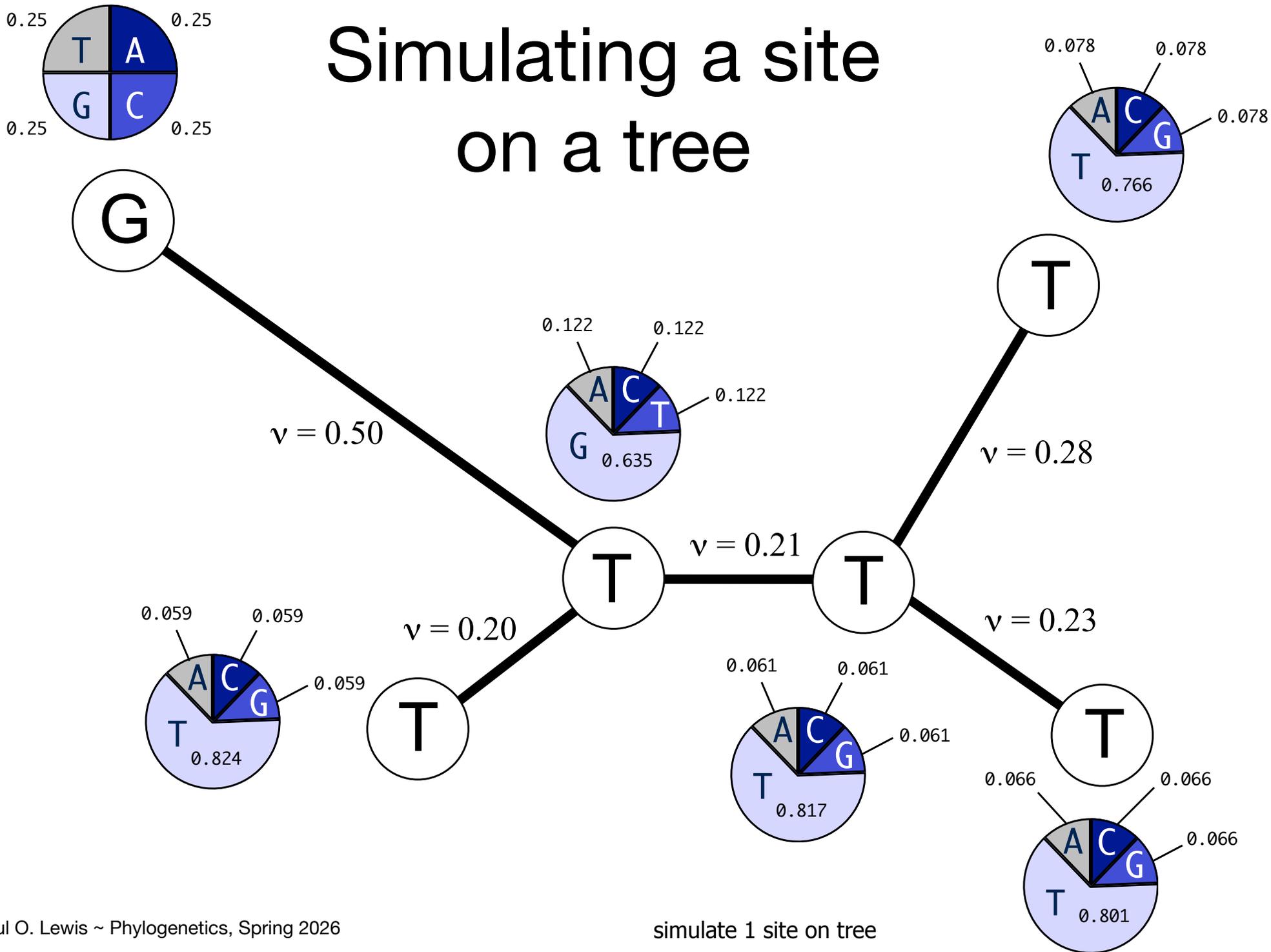
# Simulating a site on a tree



# Simulating a site on a tree



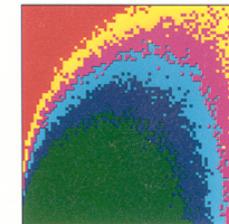
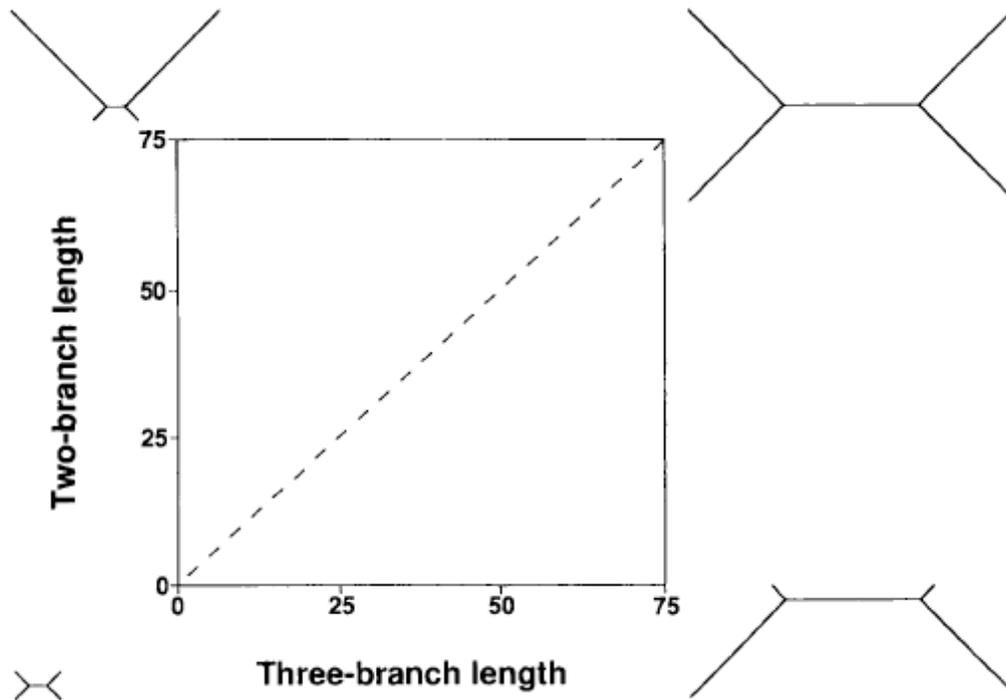
# Simulating a site on a tree



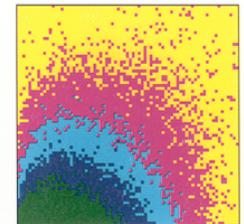
# Uses of simulation in phylogenetics

Systematic Biology

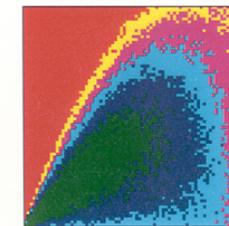
PUBLISHED BY THE  
Society of Systematic Biologists



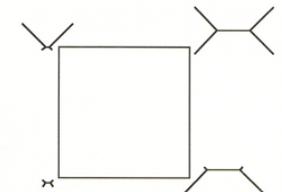
Parsimony



Lake's Invariants



UPGMA (Similarity)



Good Success Bad

VOLUME 42

SEPTEMBER 1993

NUMBER 3

Felsenstein (1978), Huelsenbeck & Hillis (1993)

## Success of Maximum Likelihood Phylogeny Inference in the Four-Taxon Case

*Brandon S. Gaut and Paul O. Lewis*

Program in Statistical Genetics, Department of Statistics, North Carolina State University

# Uses of simulation in phylogenetics

<https://imgur.com/gallery/eH0aCzk>



**megabat**



**microbat**

**one or two origins of bats?**

<https://www.milkwood.net/2015/09/21/how-to-build-a-microbat-box/>

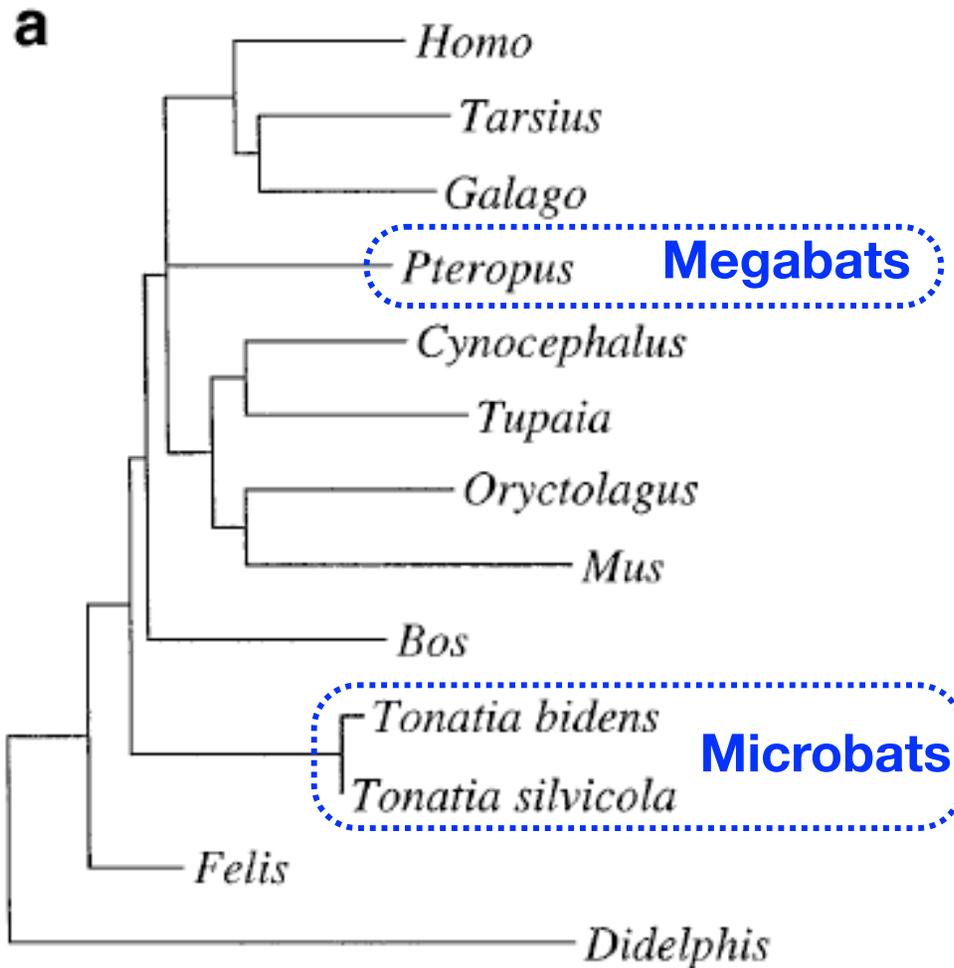
# Bat monophyly test: background

- Most phylogenetic studies concluded bats monophyletic (microbats and megabats together)
- Pettigrew argued megabats related instead to primates (megabats were “flying primates”)
- Pettigrew: apparent monophyly is an artifact: high AT composition of all bats leads to “base compositional attraction”
- Test by simulating data under null (flying primate) hypothesis (assuming strong AT bias in bat lineages) and see how often bat monophyly occurs in phylogenetic analyses

Pettigrew (1991)

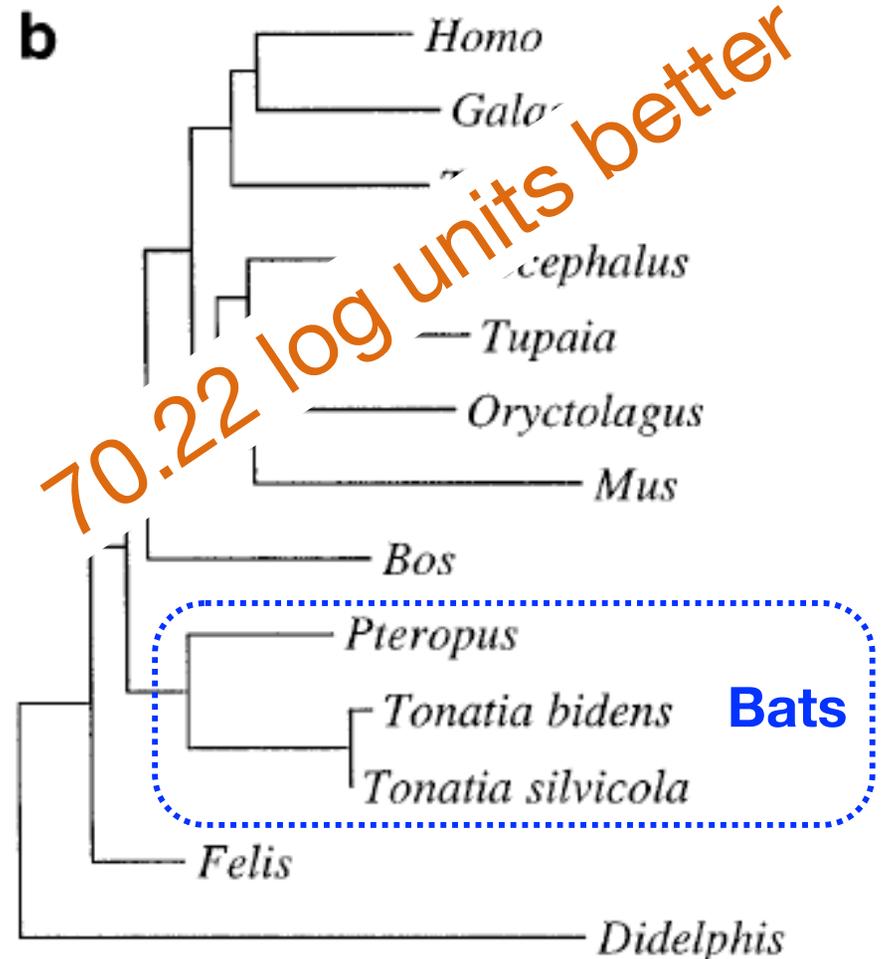
# Bat monophyly example

Null hypothesis



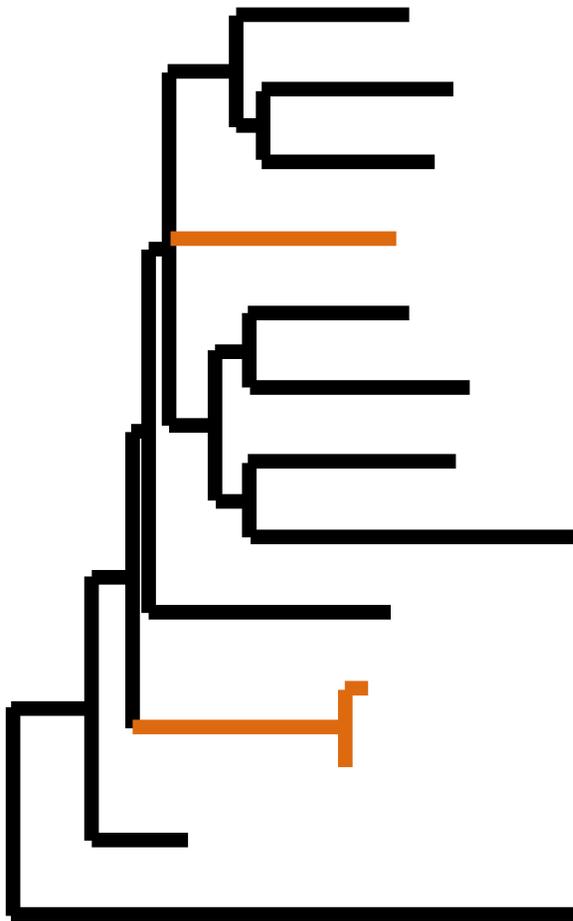
Constrained (log  $L = -6316.83$ )

Alternative hypothesis (ML tree)



Unconstrained (log  $L = -6246.61$ )

# Simulating base-compositional attraction attraction



JC69 model applies to **black** lineages only

F81 model applies to **orange** lineages only

$$\pi_A = \pi_T = 0.4$$

$$\pi_C = \pi_G = 0.1$$

# Bat monophyly example

